
Testing Climate Models with GNSS Radio Occultation

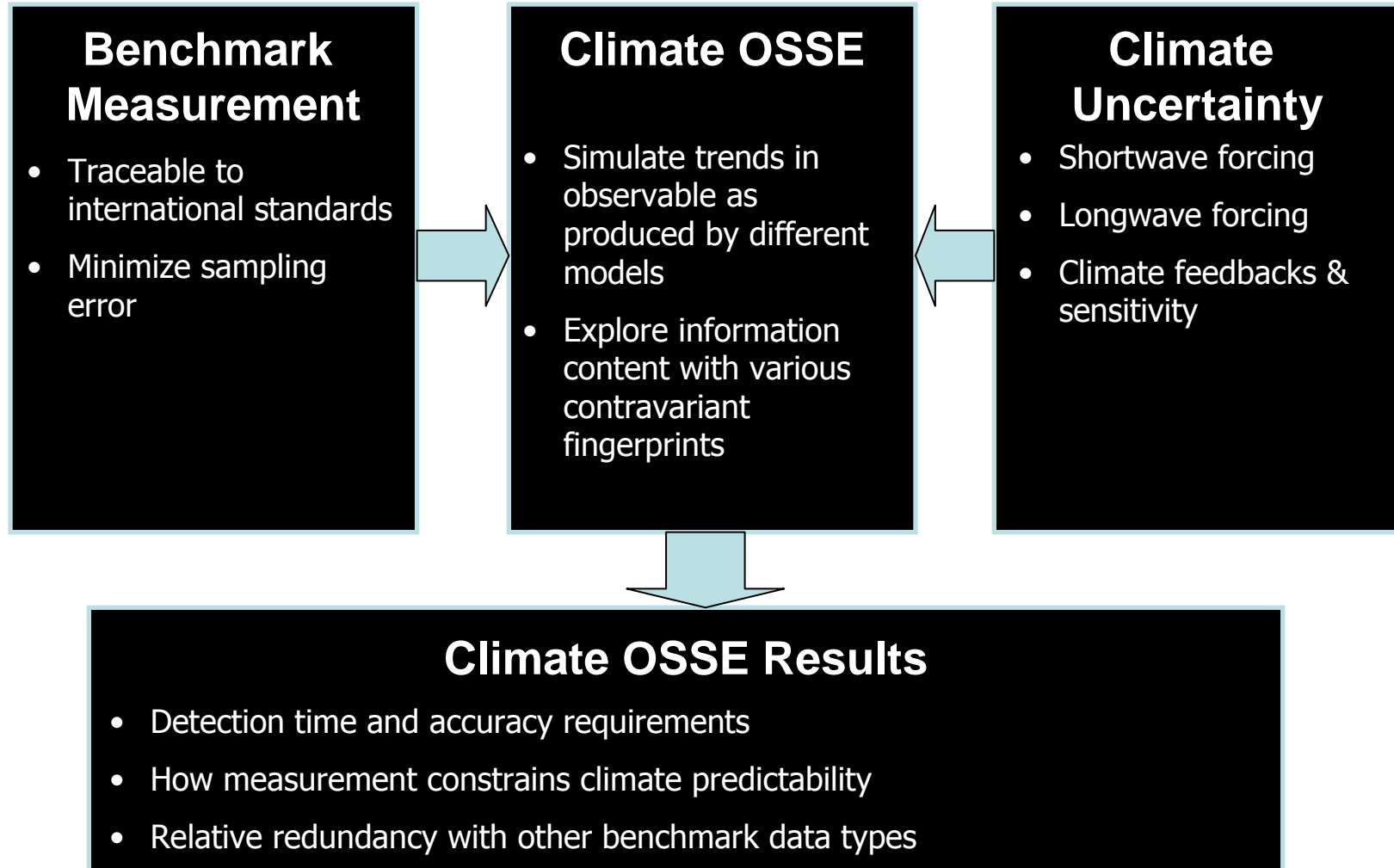
Stephen Leroy, John Dykema, Jim Anderson
Harvard University, Cambridge, Massachusetts

7 April 2009

Talk Outline

- Climate OSSE
 - Optimal Methods/Multi-pattern regression
 - Response: GPS Radio Occultation (RO)
- An Approach to Accuracy Requirements
- Discussion

Climate OSSE: The Science of a Benchmark



Optimal Fingerprinting/Multi-pattern Regression

We are limited by the naturally occurring inter-annual variability of the climate system...so optimize.

Find signal amplitudes (\mathbf{a}_m) and uncertainty ($\mathbf{\Sigma}_a$) in a data set (\mathbf{d}) according to the signals' patterns (\mathbf{s}_j) against a background of natural variability, the eigenvectors and eigenvalues of which are \mathbf{e}_μ and λ_μ .

$$\frac{d\mathbf{a}}{dt} = \mathbf{G}^{-1} \mathbf{H} \frac{d\mathbf{d}}{dt}$$

$$\mathbf{\Sigma}_{d\mathbf{a}/dt} = \mathbf{G}^{-1}$$

$$\mathbf{h}_i = \sum_{\mu=1}^k \lambda_\mu^{-1} \langle \mathbf{e}_\mu, \mathbf{s}_i \rangle \mathbf{e}_\mu$$

$$G_{i,j} = \langle \mathbf{h}_i, \mathbf{s}_j \rangle$$

GPS Radio Occultation

- Refractivity

$$N = (n - 1) \times 10^6 = (77.6 \text{ K hPa}^{-1}) \frac{p}{T} + (363 \times 10^3 \text{ K}^2 \text{ hPa}^{-1}) \frac{p_w}{T^2}$$

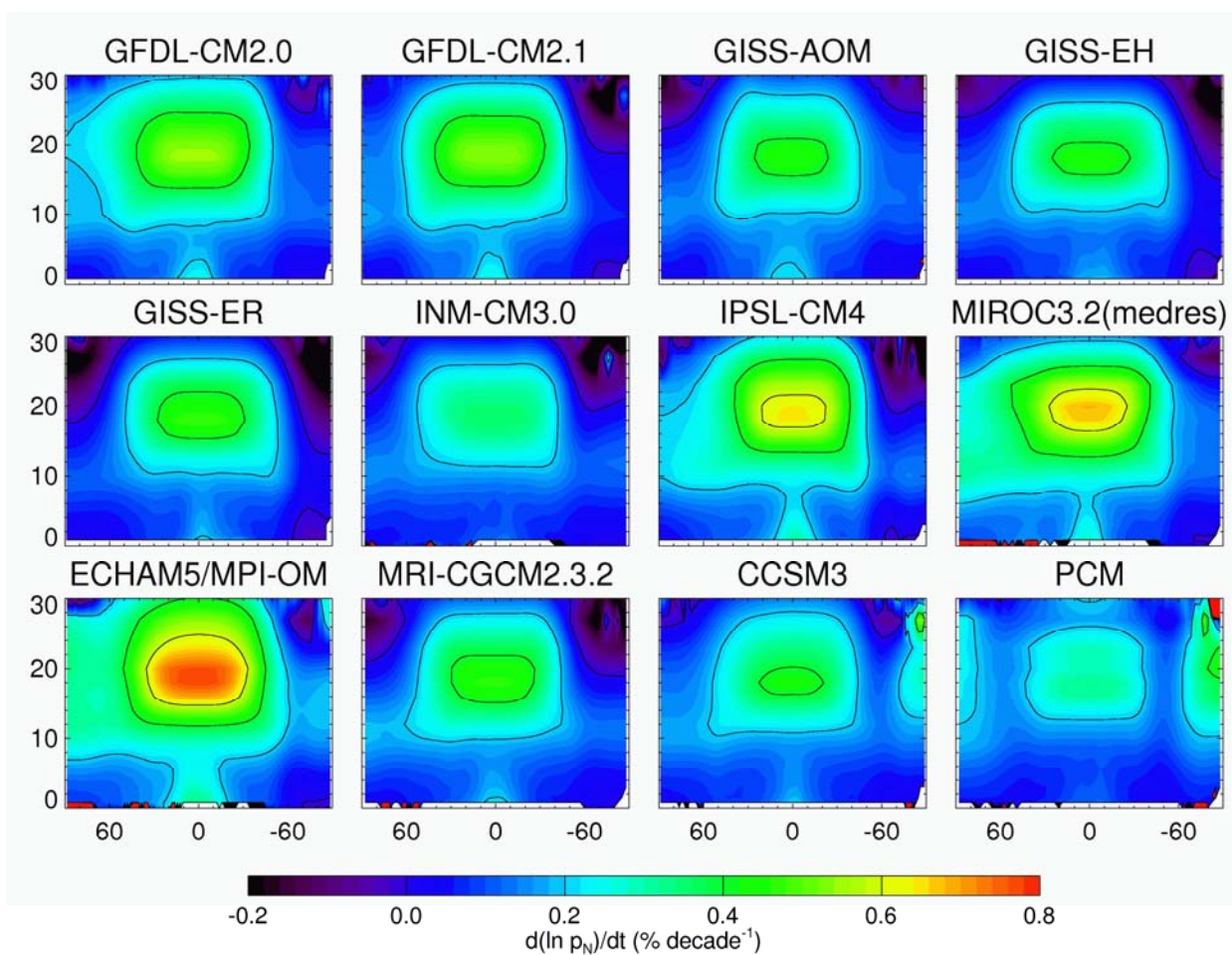
- “Dry” pressure

$$p_d(h) = (4.402 \times 10^{-4} \text{ hPa m}^{-1}) \int_h^{\infty} N dh \cong p(h) + (7521 \text{ K}) \int_0^{p(h)} \frac{q dp}{T}$$

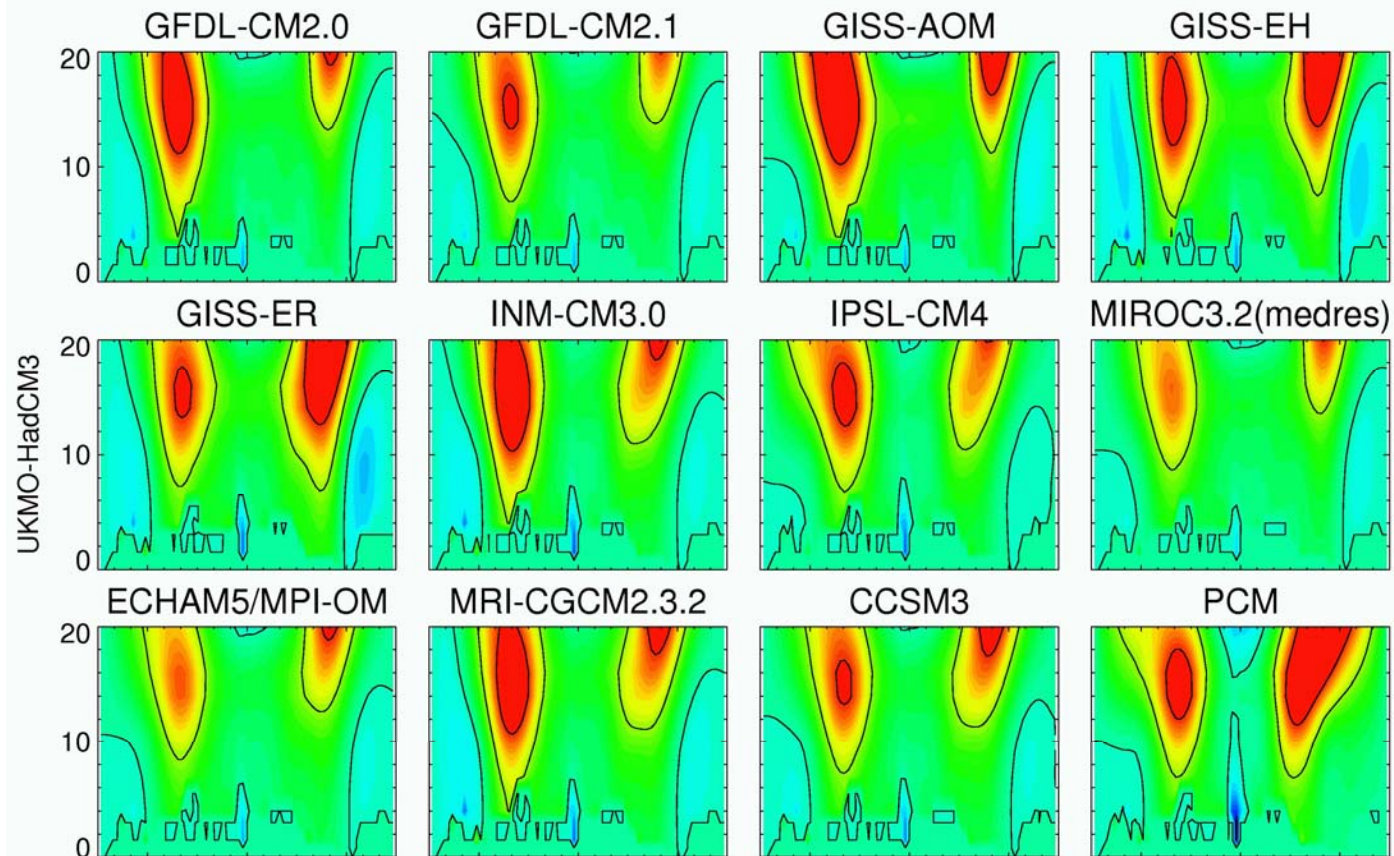
- Geopotential height

$$h = \left[(\Phi(\mathbf{r}) - \frac{1}{2} \Omega^2 r_s^2) - (\Phi - \frac{1}{2} \Omega^2 r_s^2)_{\text{msl}} \right] / g_0$$

GPS RO Dry Pressure Tendency



Fingerprints



95% Detection Times

| Model | GFDL CM2.0 (yrs) | ECHAM5/MPI-OM (yrs) | UKMO-HadCM3 (yrs) | MIROC3.2 (medres) (yrs) | Tropospheric Expansion (m decade⁻¹) |
|-------------------|-----------------------------|--------------------------------|------------------------------|--|---|
| GFDL-CM2.0 | 8.67 | 9.05 | 8.29 | 6.63 | 11.02 |
| GFDL-CM2.1 | 7.88 | 8.65 | 7.57 | 6.21 | 12.86 |
| GISS-AOM | 10.53 | 11.54 | 10.47 | 8.38 | 9.67 |
| GISS-EH | 10.41 | 11.74 | 10.77 | 8.50 | 9.12 |
| GISS-ER | 10.89 | 12.70 | 11.07 | 9.32 | 8.79 |
| INM-CM3.0 | 9.98 | 11.23 | 9.79 | 8.15 | 10.71 |
| IPSL-CM4 | 9.29 | 10.02 | 8.95 | 7.36 | 10.54 |
| MIROC 3.2(medres) | 7.09 | 7.47 | 6.83 | 5.39 | 13.04 |
| ECHAM5/MPI-OM | 7.78 | 8.16 | 7.45 | 5.87 | 12.34 |
| MRI-CGCM2.3.2 | 9.95 | 11.70 | 9.92 | 8.35 | 10.68 |
| CCSM3 | 8.87 | 9.62 | 8.68 | 6.80 | 11.97 |
| PCM | 12.69 | 12.32 | 11.95 | 8.45 | 7.27 |

Accuracy Requirements, Detection Times

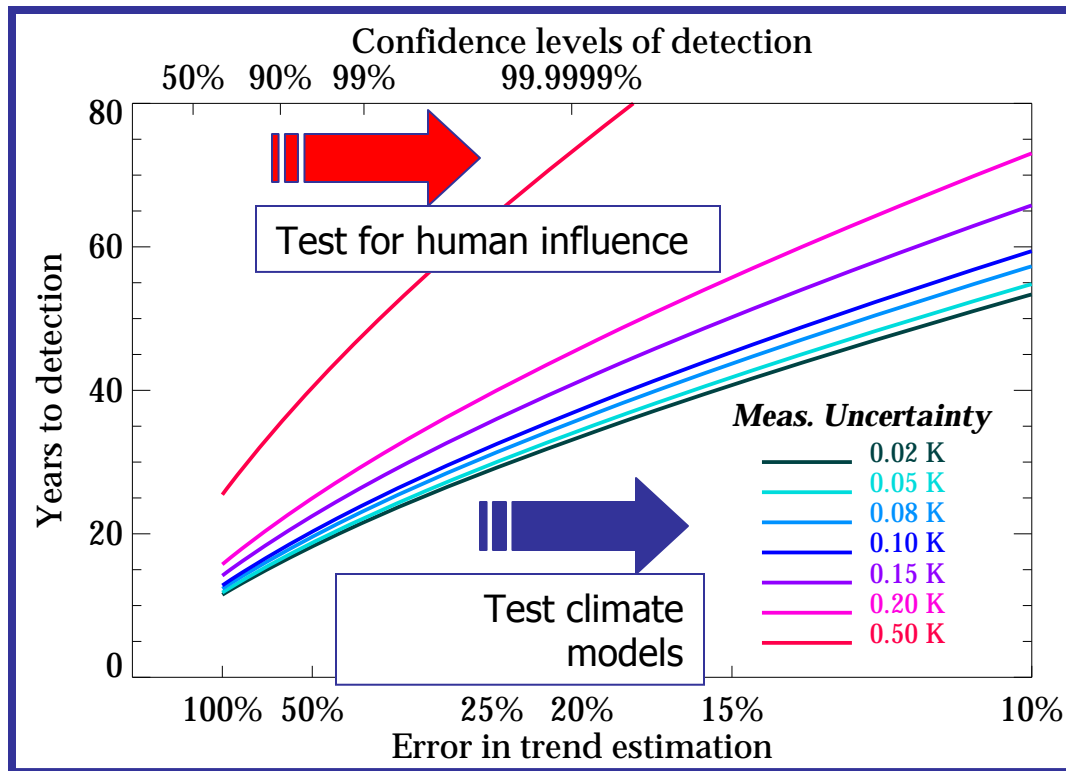
- With observations traceable to international standards, one evaluates the uncertainty (accuracy) of individual measurements in a timeseries.
- Any timeseries of climate data includes both natural variability with standard deviation σ_v , timescale τ_v , and measurement uncertainty (σ_m and τ_m).

With a timeseries of length Δt , the uncertainty in the determination of the slope determination is

$$\delta m^2 = 12 (\Delta t)^{-3} \left(\sigma_v^2 \tau_v + \sigma_m^2 \tau_m \right)$$

Leroy, S.S., J.G. Anderson, and G. Ohring, 2008: Climate signal detection times and constraints on climate benchmark accuracy requirements. *J. Climate*, **21**, 841-846.

Measurement Uncertainty & Detection Times



Global temperature at 500 hPa

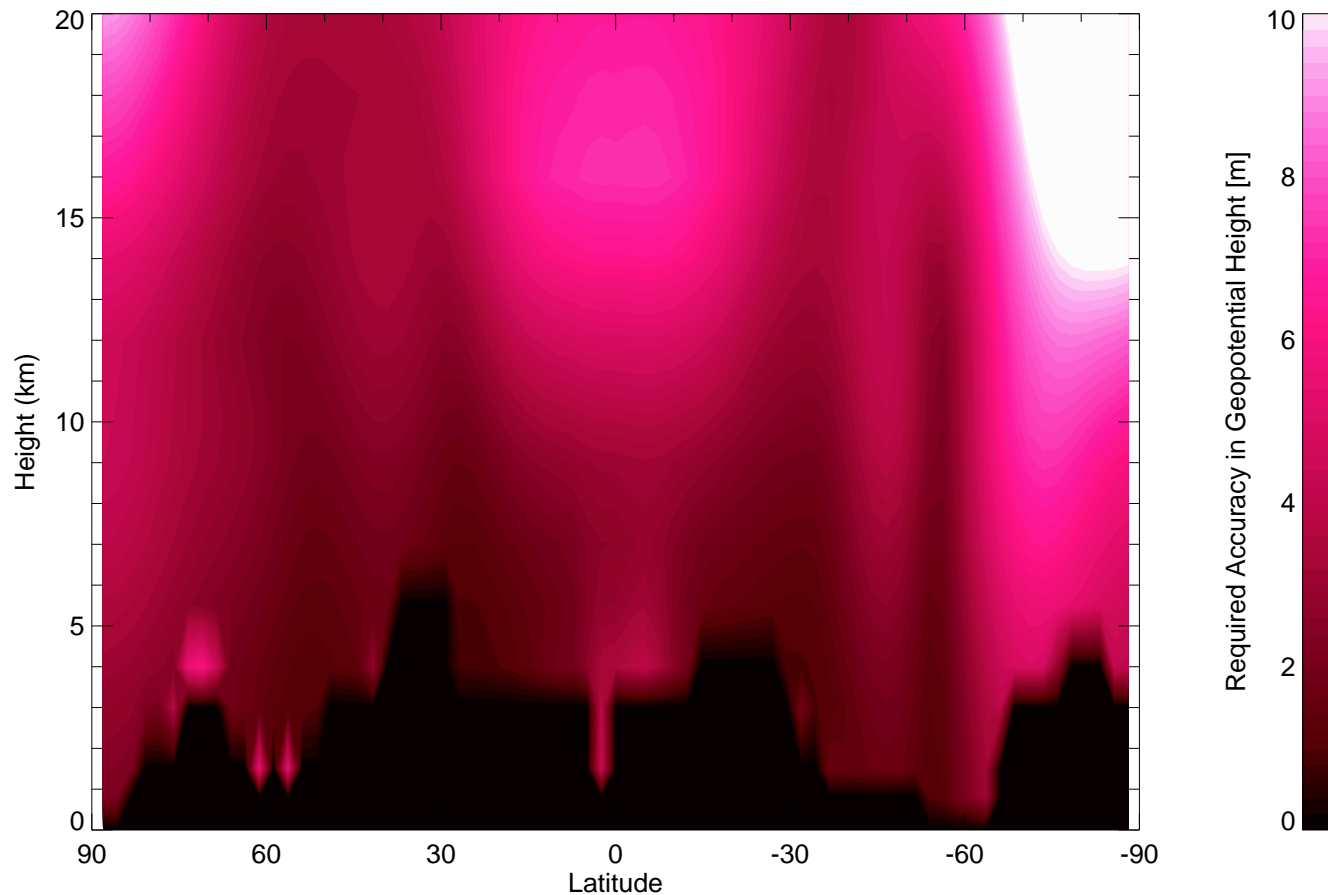
Three satellites, 6-year lifetime.

Natural variability: 0.18 K, 1.54 year correlation time (UKMO HadCM3),
Trend: $\sim 0.2 \text{ K decade}^{-1}$.

Optimization has the effect of lowering the entire family of curves.

GNSS RO, 6-yr Mission

Accuracy requirements for a 6-yr mission, based on UKMO HadCM3 control



Summary

- GNSS RO has the unique capability of measuring thermal expansion of the troposphere
- First signal detected is poleward migration of baroclinic zones
- Accuracy requirement for lower troposphere is a few parts in 10^4 for refractivity
- Accuracy requirements for stratosphere yet to be determined.

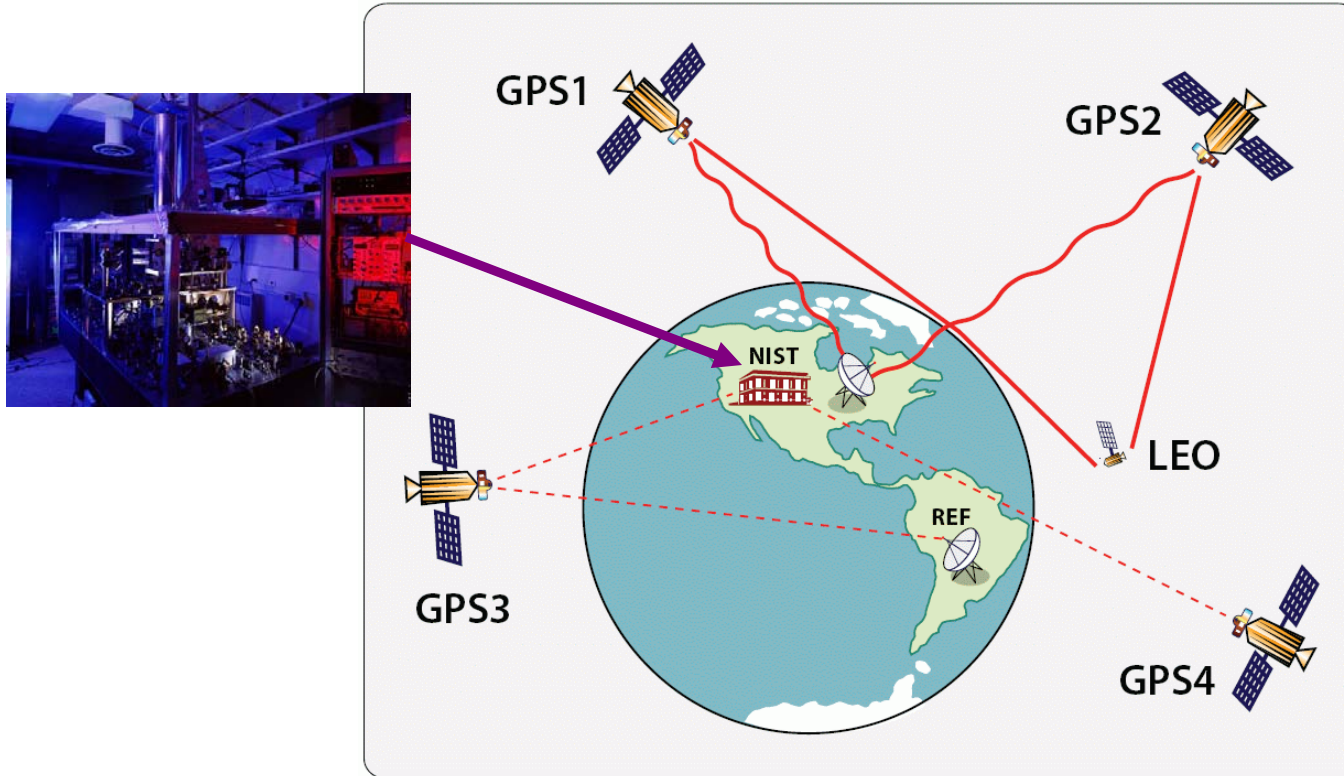
Acknowledgments: NSF Atmospheres Program, NASA
CLARREO Project

Extra Slides

Sources of Error?

- Testing by inter-mission comparison
 - CHAMP vs SAC-C
 - CHAMP vs COSMIC
- Testing by inter-center trend comparison
 - Ho et al.: Dominant error is sampling error, a random term. Primary cause is quality control.
 - Natural to better understand QC for GPS RO, but may not be necessary for climate.
- Residual ionosphere:
 - Large scale?
 - Scintillation and nonlinearity?

Calibration: SI Traceability



Double differencing

Hardy, K.R., G.A. Hajj, and E.R. Kursinski, 1994: Accuracies of atmospheric profiles obtained from GPS occultations. *Int. J. Sat. Comm.*, **12**, 463-473.

Thermal Infrared Spectra

