

Satellite Drag Environment Prediction: Leveraging Data-Assimilative Driver Estimates

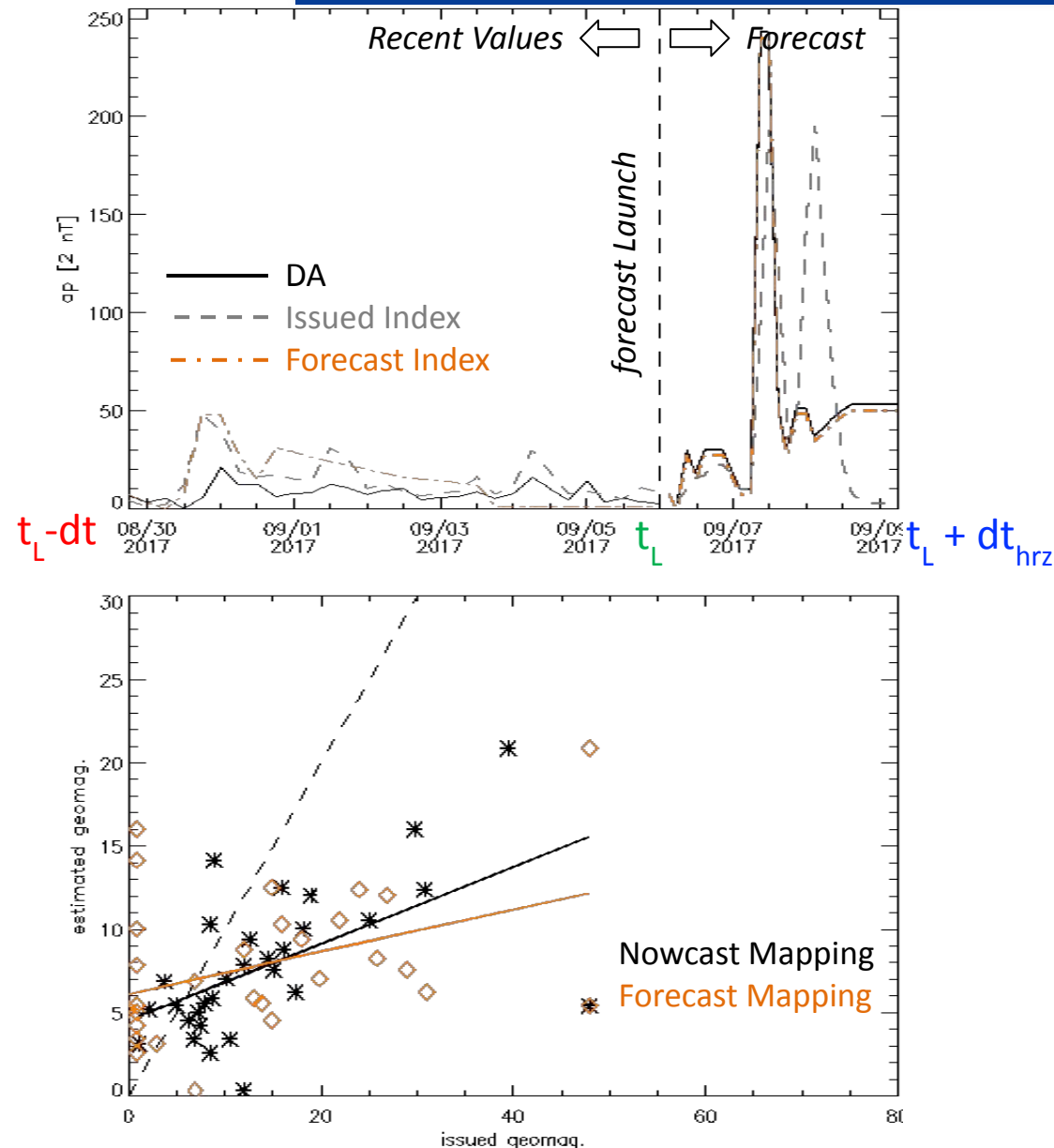
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¹LASP, University of Colorado, ²SWxTREC, ³Space Environment Technologies, ⁴Orion Space Solutions LLC.

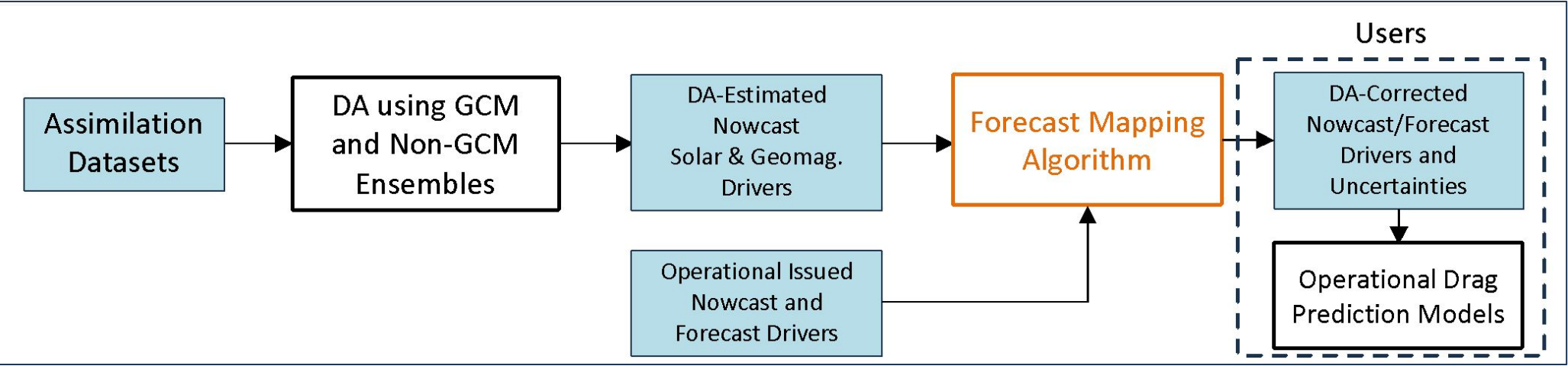
Wednesday 2025-09-10

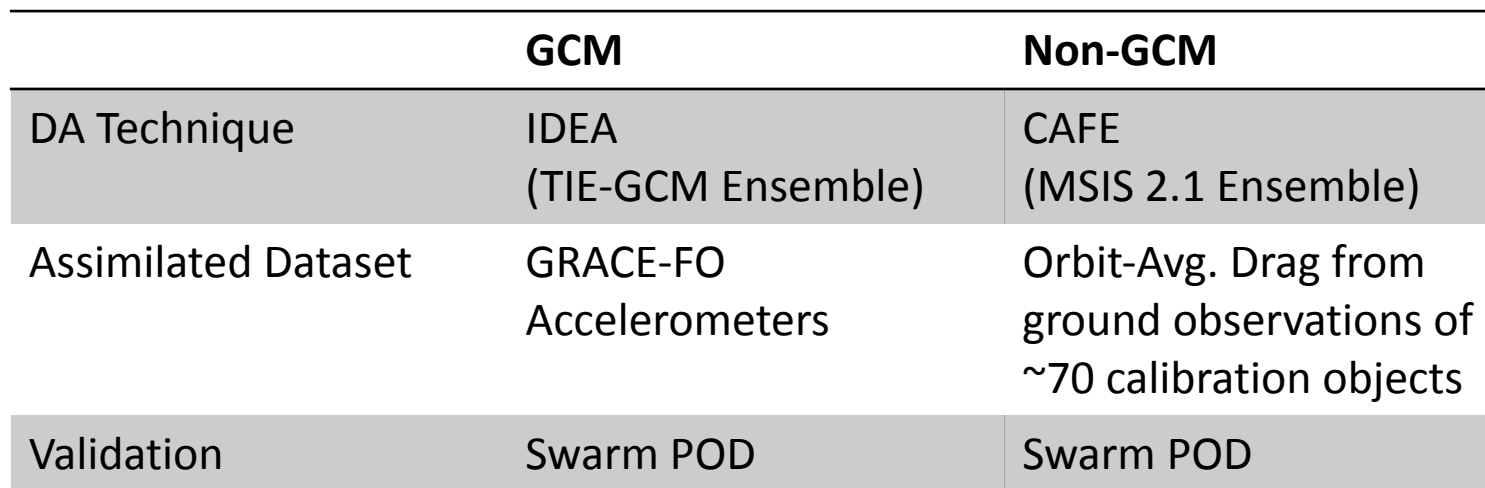
Boulder, CO

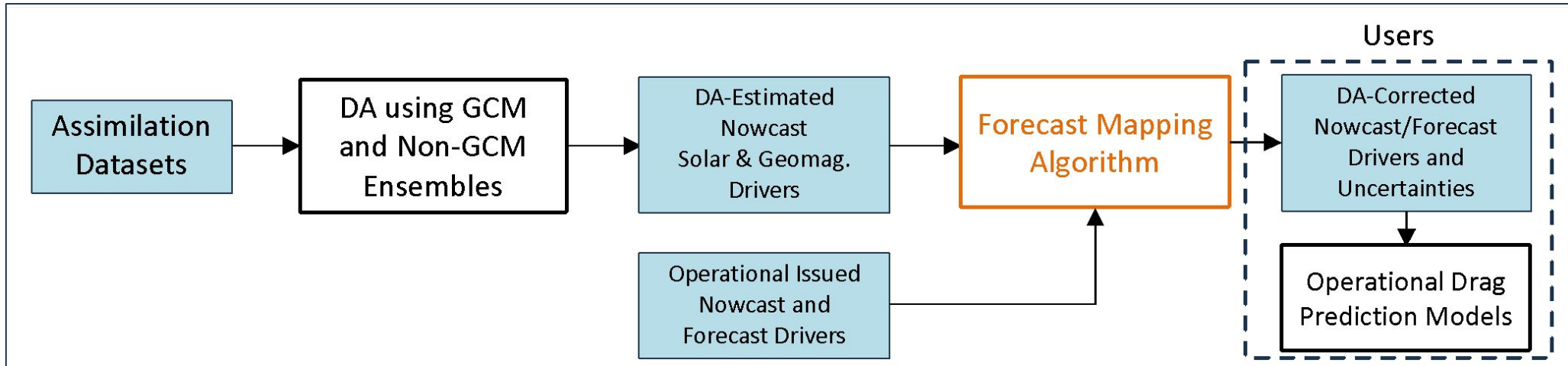
Funded by NASA R202R



- Simple approach: remove bias between estimated and nowcast/forecast states at the time of the forecast launch, t_L
- Some neutral density forecasting approaches use bias offset and regression methods to compute forecasts
- The bottom panel illustrates a linear-regression mapping of the recently issued $[t_L - dt, t_L]$ nowcast from (black) and forecast (orange) to the DA-estimated drivers. **This mapping changes with time and conditions**
- ***How best to take advantage of recent DA driver estimates and recent forecast forcing performance?***

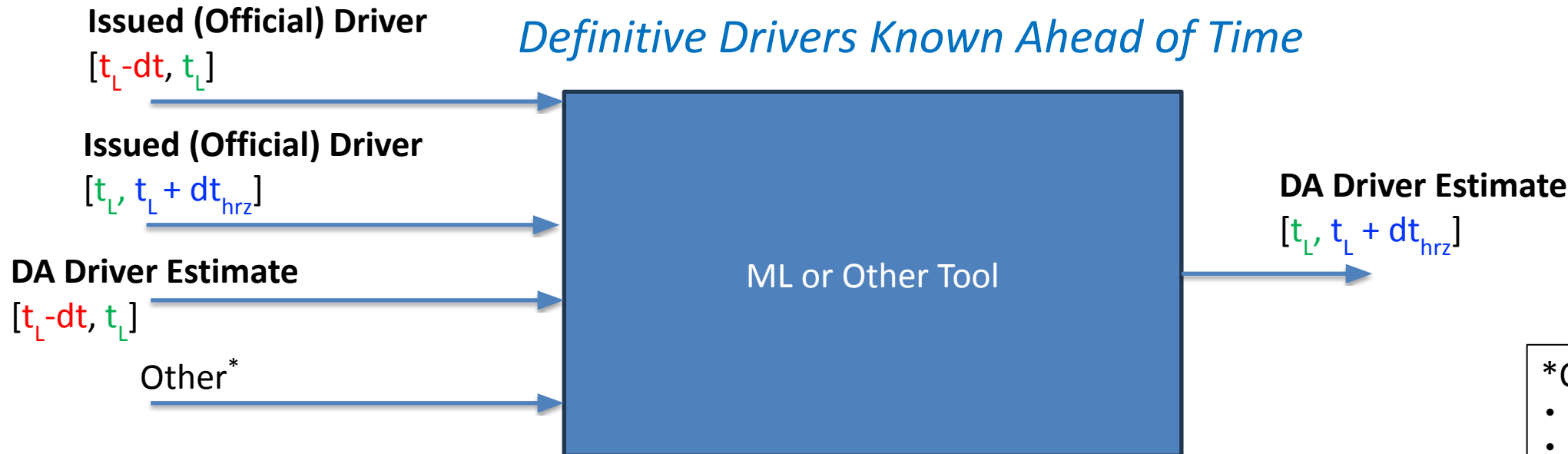




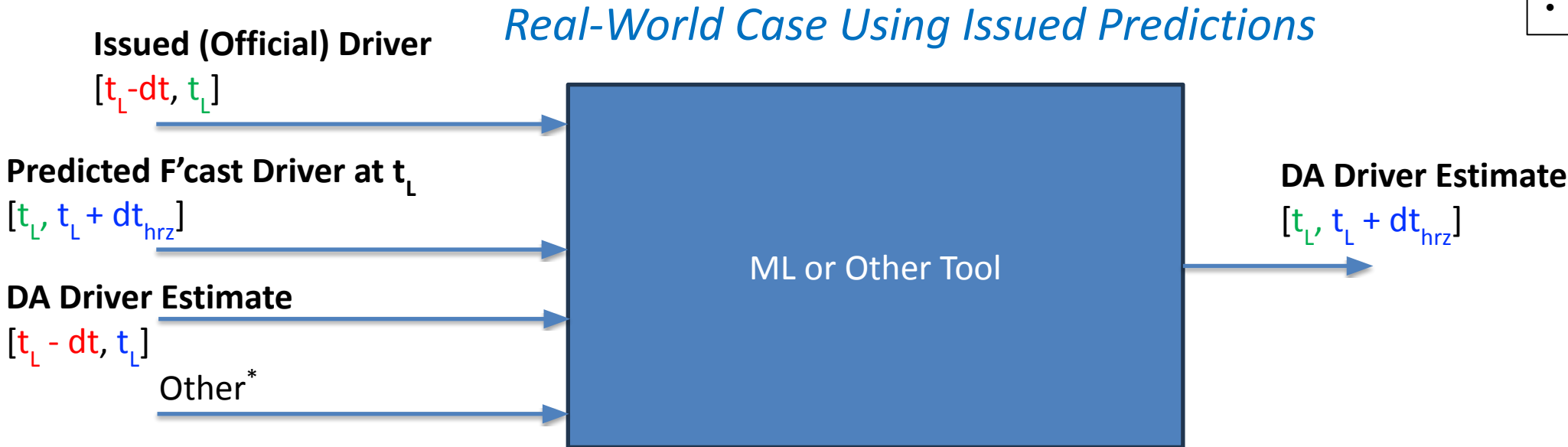


Project Objectives:

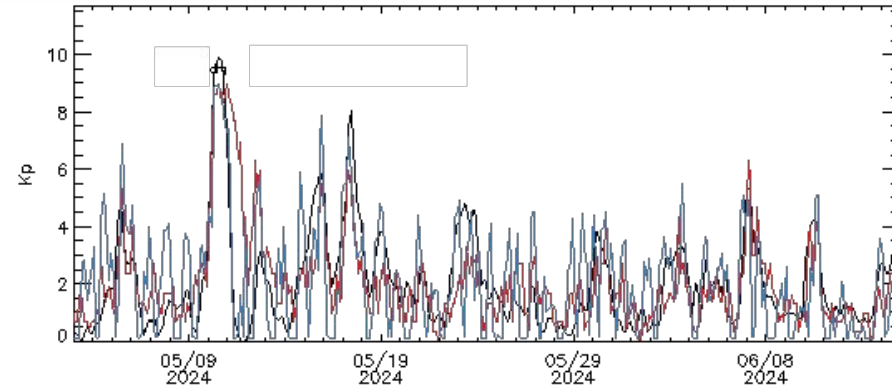
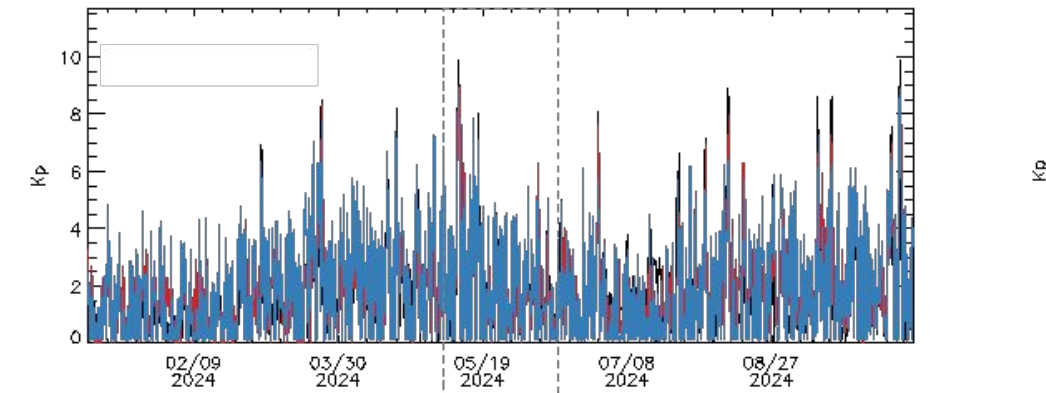
- (a) Identify methodologies to map data-assimilative estimates of solar and geomagnetic drivers to operational forecast streams.
- (b) Evaluate the results using metrics relevant to LEO orbit forecasting over several years.



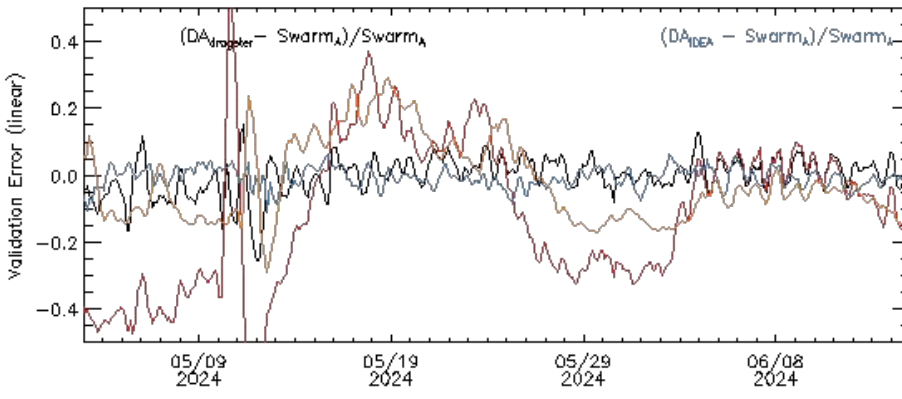
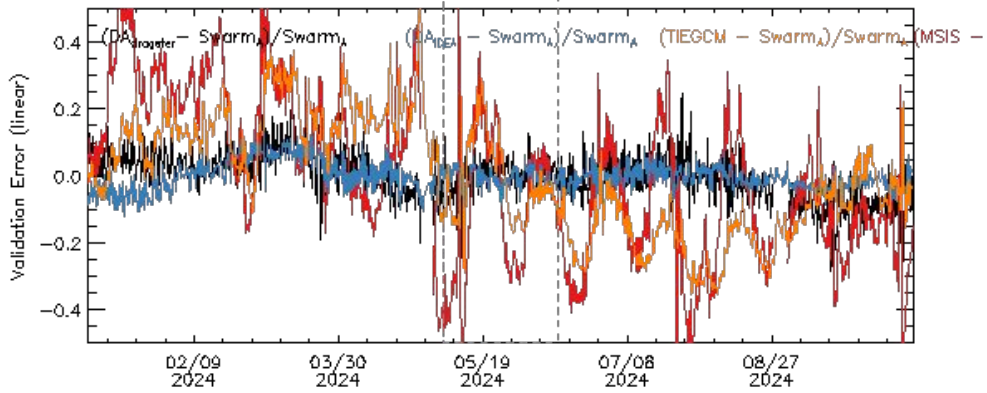
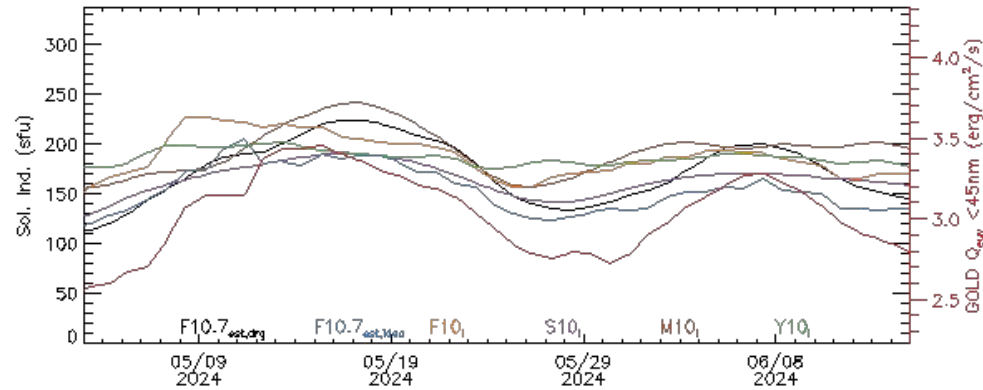
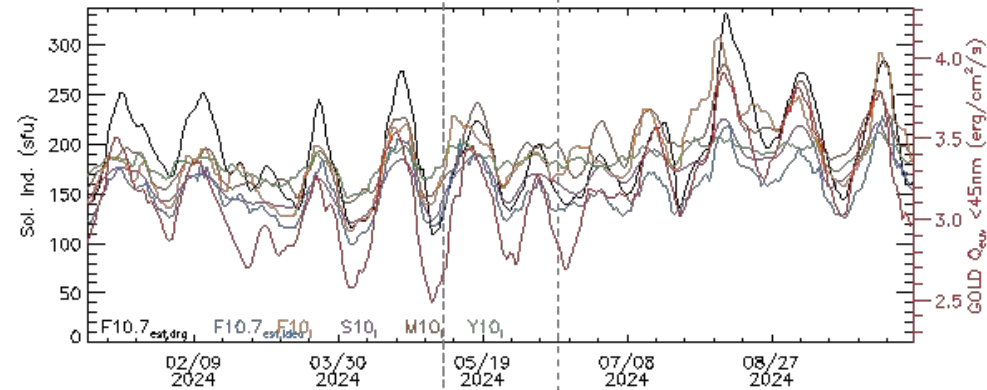
- *Other
- Season/Day of Year
 - Time of Day
 - 81-day trailing solar
 - ...



Examples of Post-Storm Discrepancy

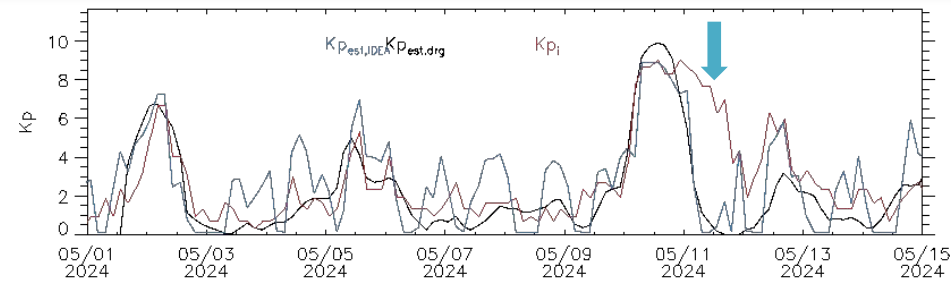
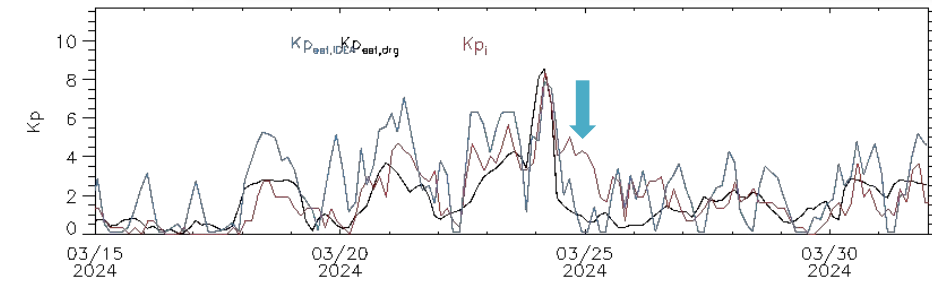


CAFE 1.0 (MSIS)
IDEA (TIEGCM)
Issued Kp

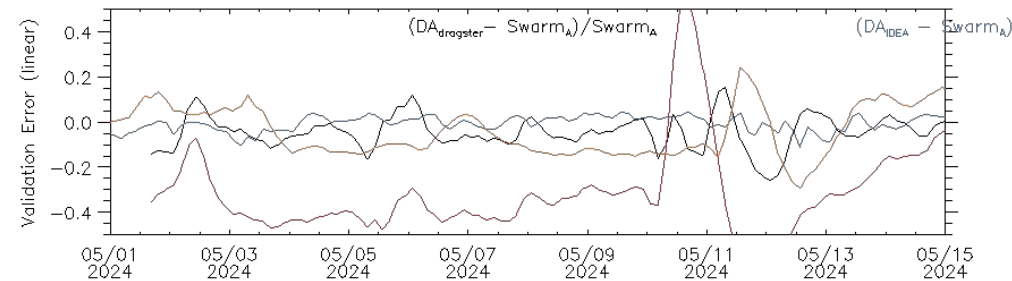
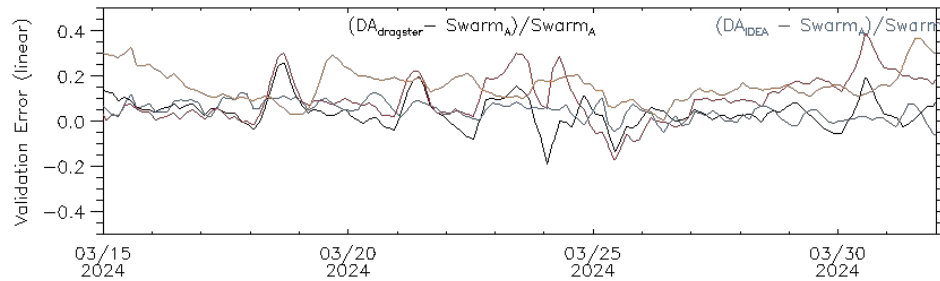
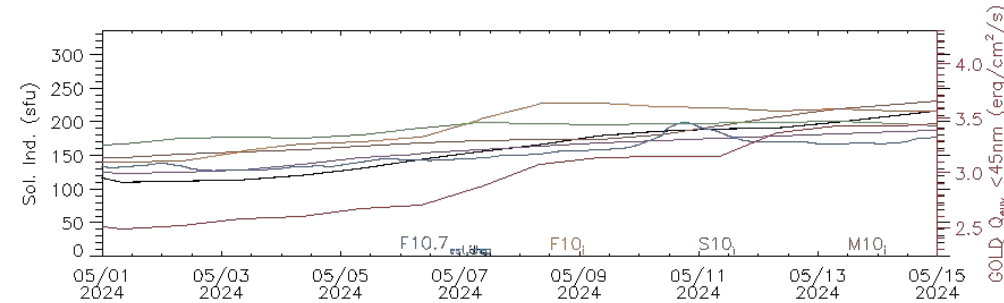
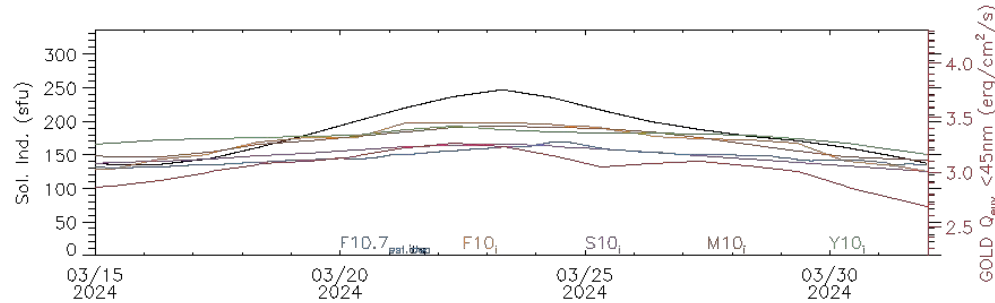


CAFE 1.0 (MSIS)
IDEA (TIEGCM)
TIEGCM_{GPI}
NRLMSISE-2.1

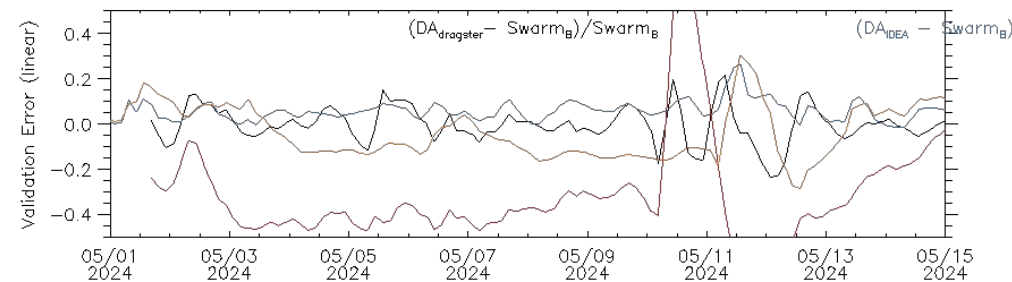
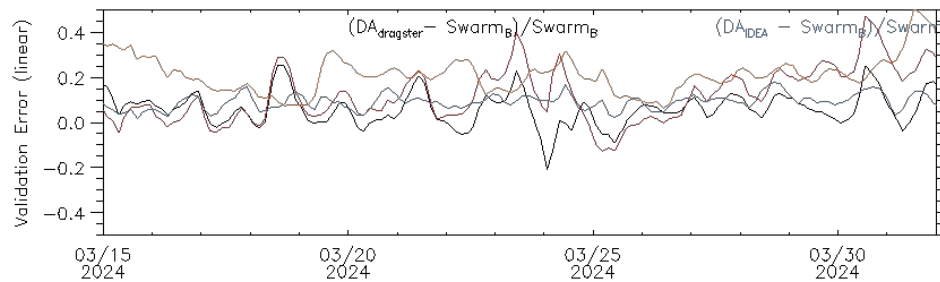
Examples of Post-Storm Discrepancy



CAFE 1.0 (MSIS)
IDEA (TIEGCM)
Issued Kp



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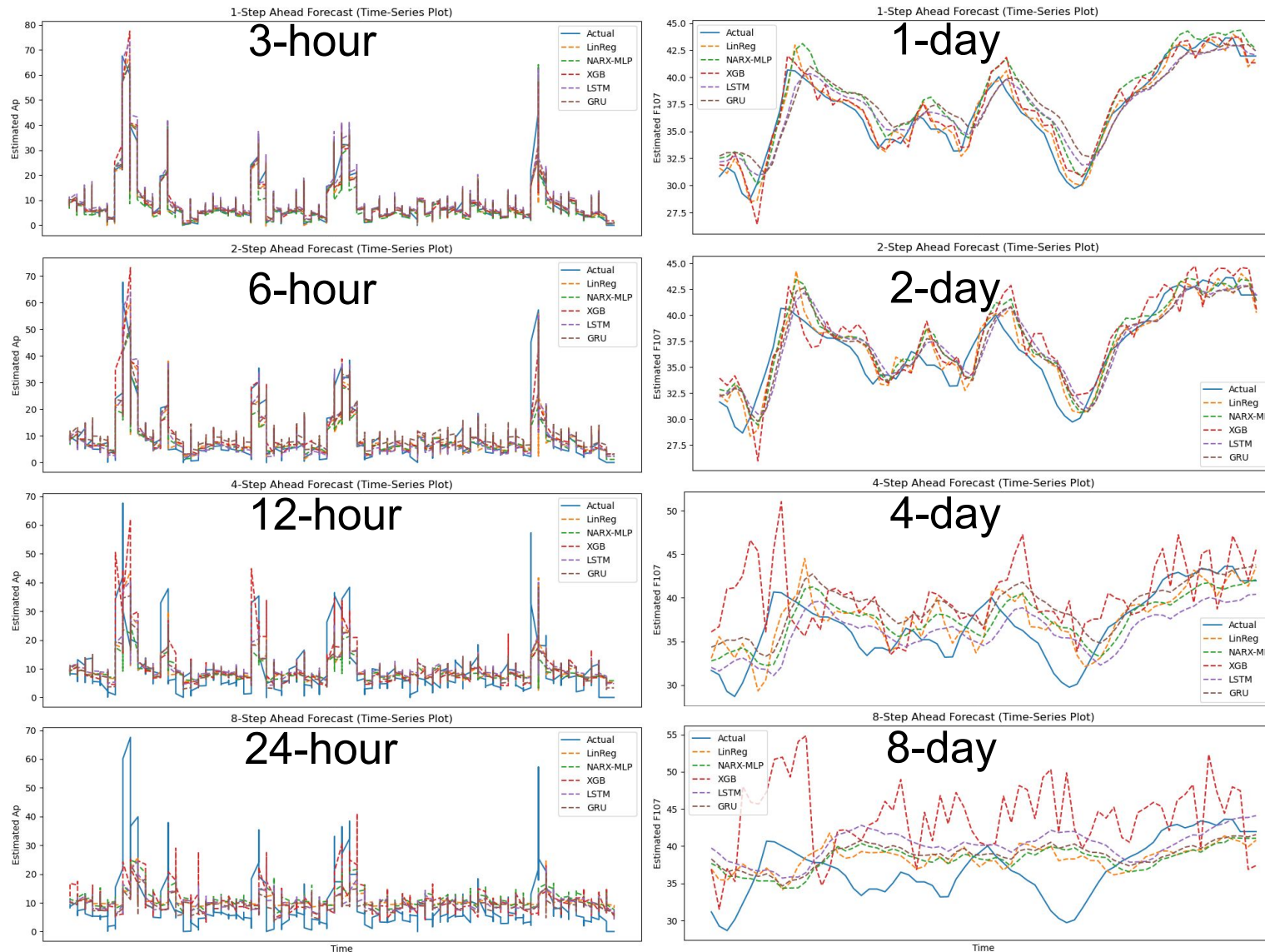
CAFE 1.0 (MSIS)
IDEA (TIEGCM)
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| 2024 Validation Results, StdDev Logarithmic | | | | |
|---|----------------------------|---------|----------------------------|---------|
| | Swarm-A (~480 km altitude) | | Swarm-B (~520 km altitude) | |
| | 1 Orbit | ¼ Orbit | 1 Orbit | ¼ Orbit |
| IDEA | 0.042 | 0.095 | 0.078 | 0.126 |
| Dragster 1.0 | 0.066 | 0.107 | 0.059 | 0.110 |
| Dragster 1.0 DC* | 0.063 | 0.100 | 0.057 | 0.103 |
| TIE-GCM GPI | 0.287 | 0.323 | 0.311 | 0.353 |
| MSIS | 0.142 | 0.170 | 0.144 | 0.177 |

**Density Corrected (DC), estimating both drivers and density corrections*

| Algorithm | Strengths | Weaknesses |
|---|---|---|
| Multiple linear regression | Simple, fast, interpretable Easy to implement & explain Effective when data is near-linear or has strong autocorrelation at lag=1 | Only captures linear relationships Struggles with nonlinear, long-lag effects Sensitive to outliers |
| NARX-MLP (Nonlinear autoregressive with external input) | Capable of modeling nonlinearities Can ingest multiple lagged inputs & exog Flexible architecture (number of layers) | May require careful feature engineering Can overfit if not enough data/regularized |
| XGBoost (Extreme Gradient Boosting) | Strong performance in many tabular tasks Automatically handles some nonlinearities | Can require extensive hyperparameter tuning May struggle with very long-sequence dependencies |
| GRU (Gated Recurrent Units) | Similar to LSTM but typically simpler Fewer parameters than LSTM, faster to train | May still be prone to overfitting with insufficient data or poor architecture |
| LSTM (Long short-term memory) | Designed for sequence data (long lags) Remembers patterns across many timesteps | Higher complexity, slower training Tends to require a lot of data |

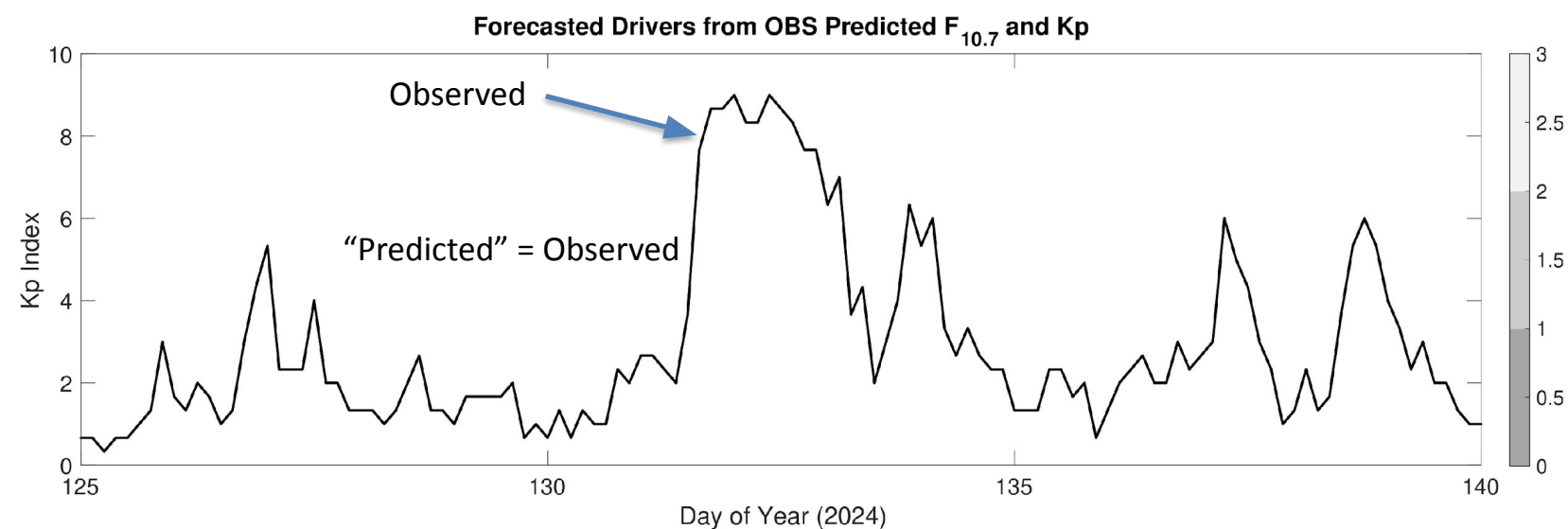
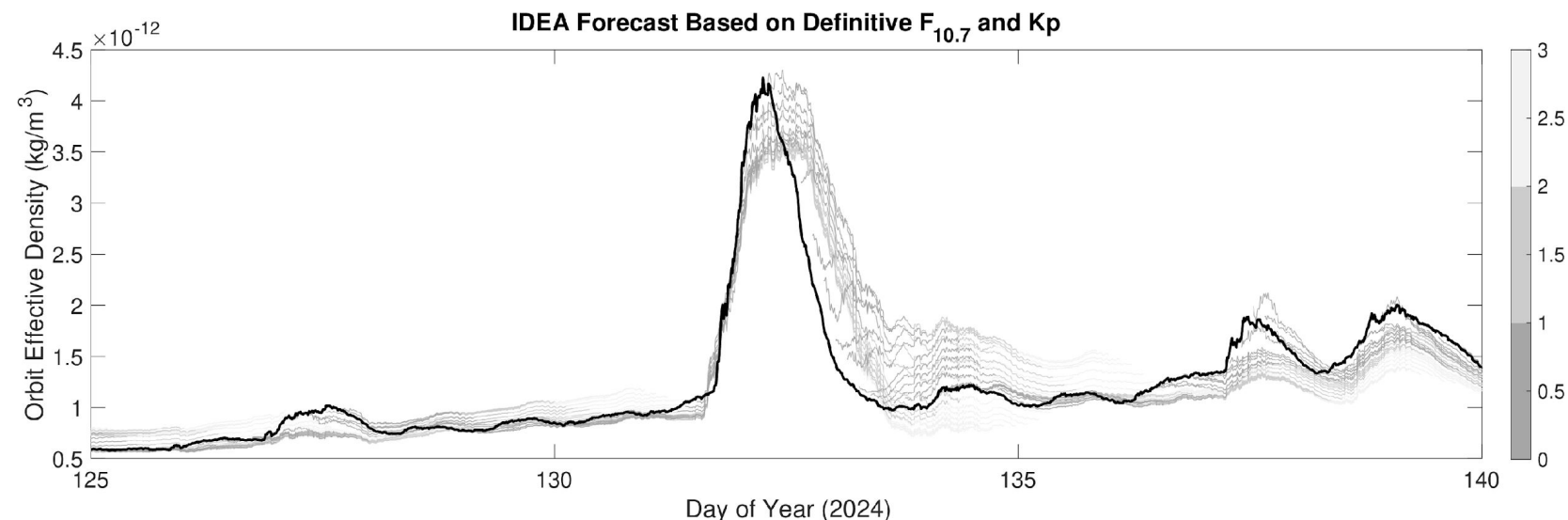
2019 Empirical-DA Predictions



IDEA (TIE-GCM) Forecast Experiments: Definitive Drivers

72-Hour “Forecast” using
Definitive Drivers:

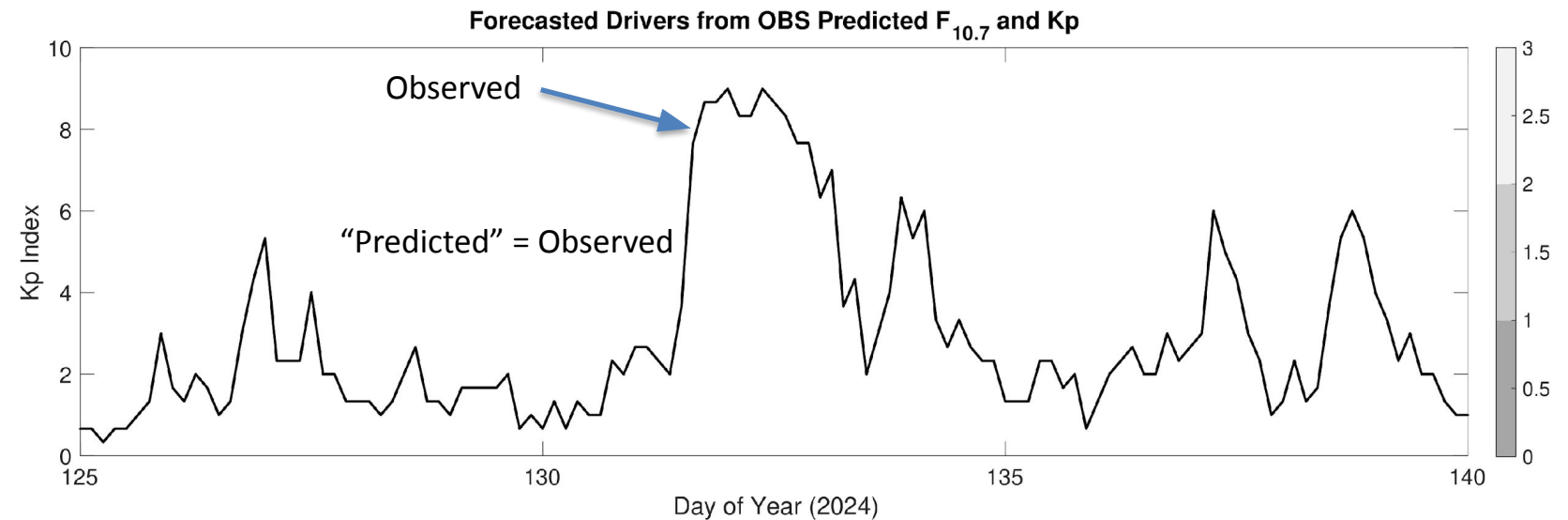
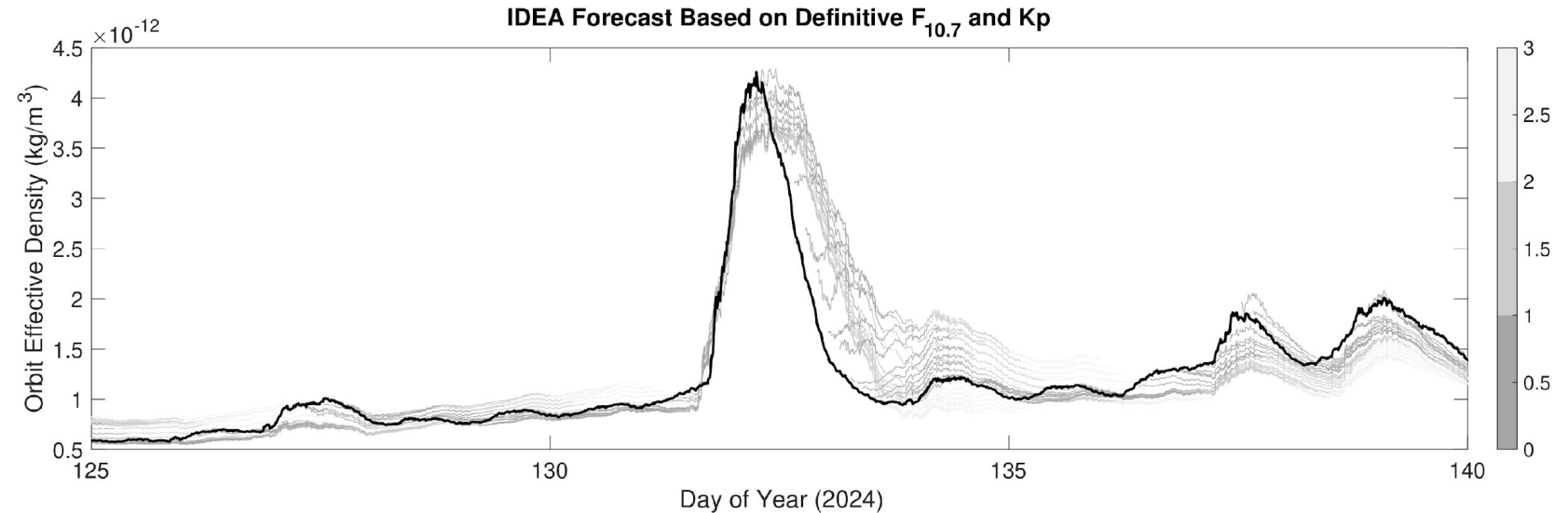
EDDYDIF: Fixed
NO Beta2: Fixed



IDEA (TIE-GCM) Forecast Experiments: Definitive Drivers

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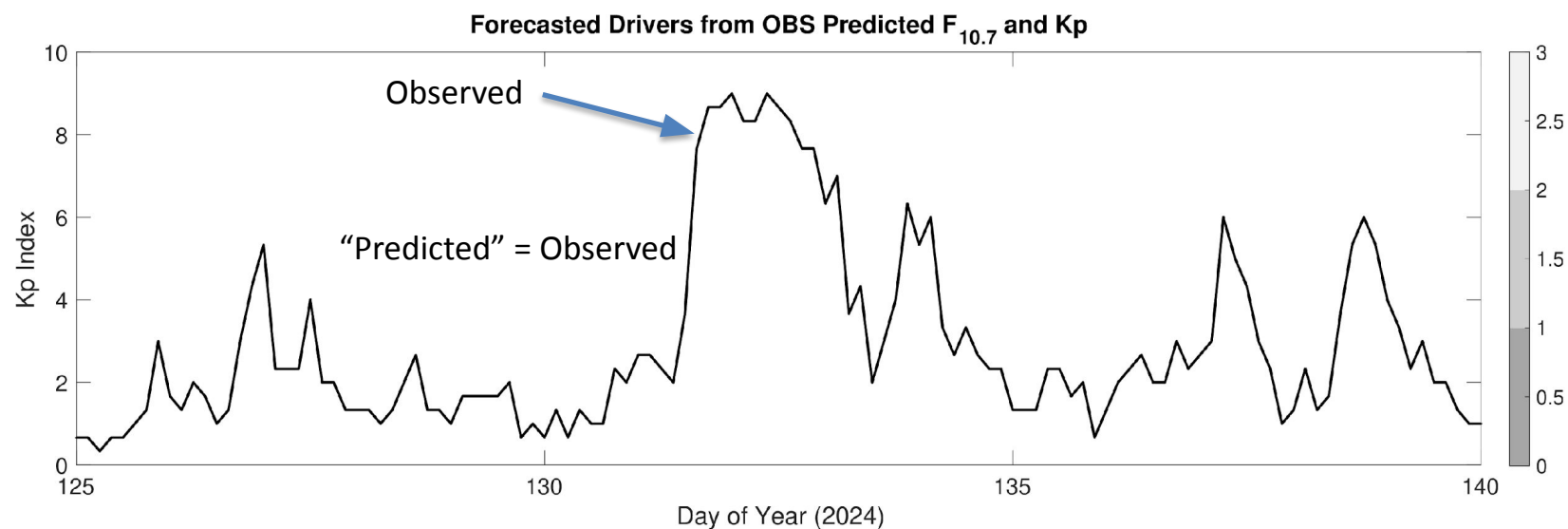
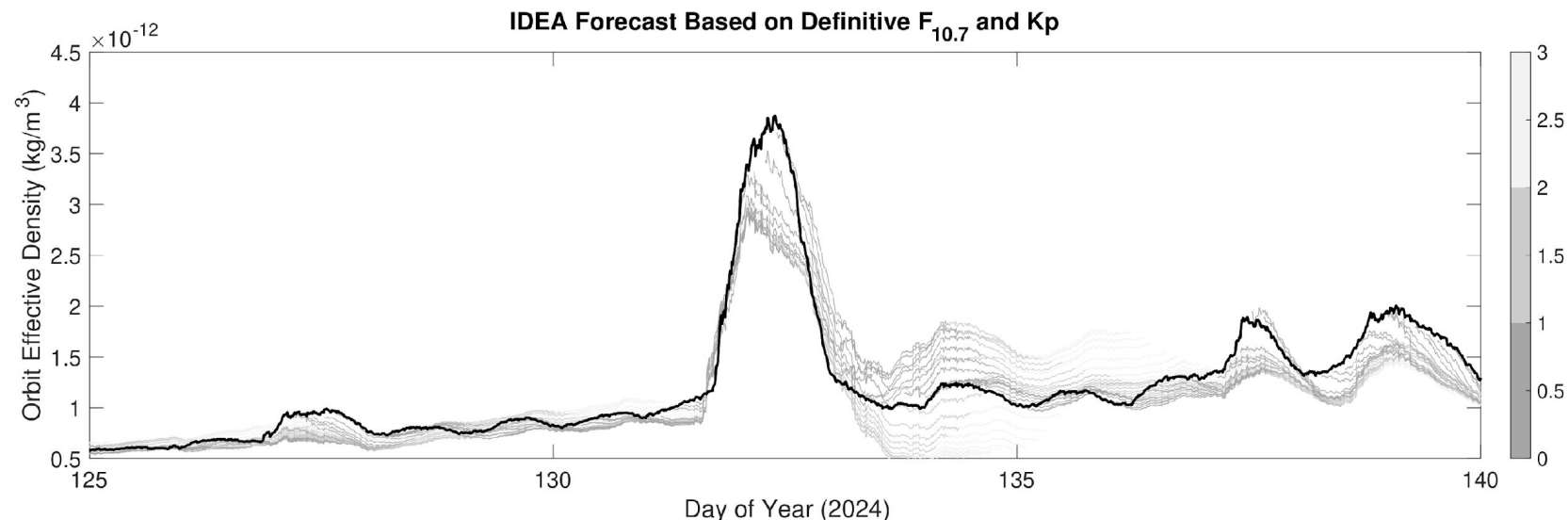
EDDYDIF: Variable
NO Beta2: Fixed



IDEA (TIE-GCM) Forecast Experiments: Definitive Drivers

72-Hour “Forecast” using
Definitive Drivers:

EDDYDIF: Variable
NO Beta2: Temperature
Dependent

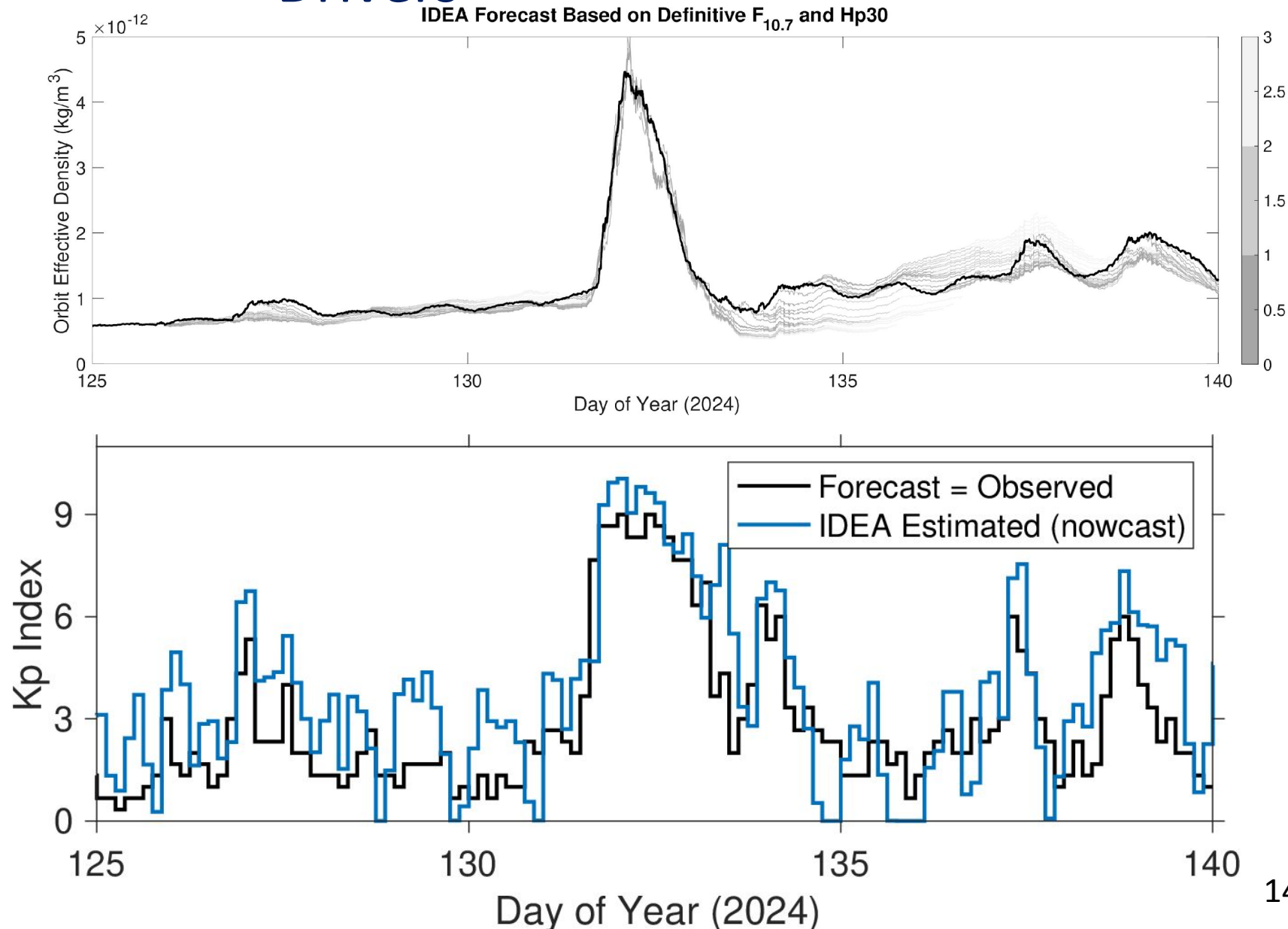


IDEA (TIE-GCM) Forecast Experiments: Definitive Drivers

72-Hour “Forecast” using
Definitive Drivers:

EDDYDIF: Variable
NO Beta2: Temperature
Dependent

Kp Bounds: Expanded
Geomag F’cst: Hp30

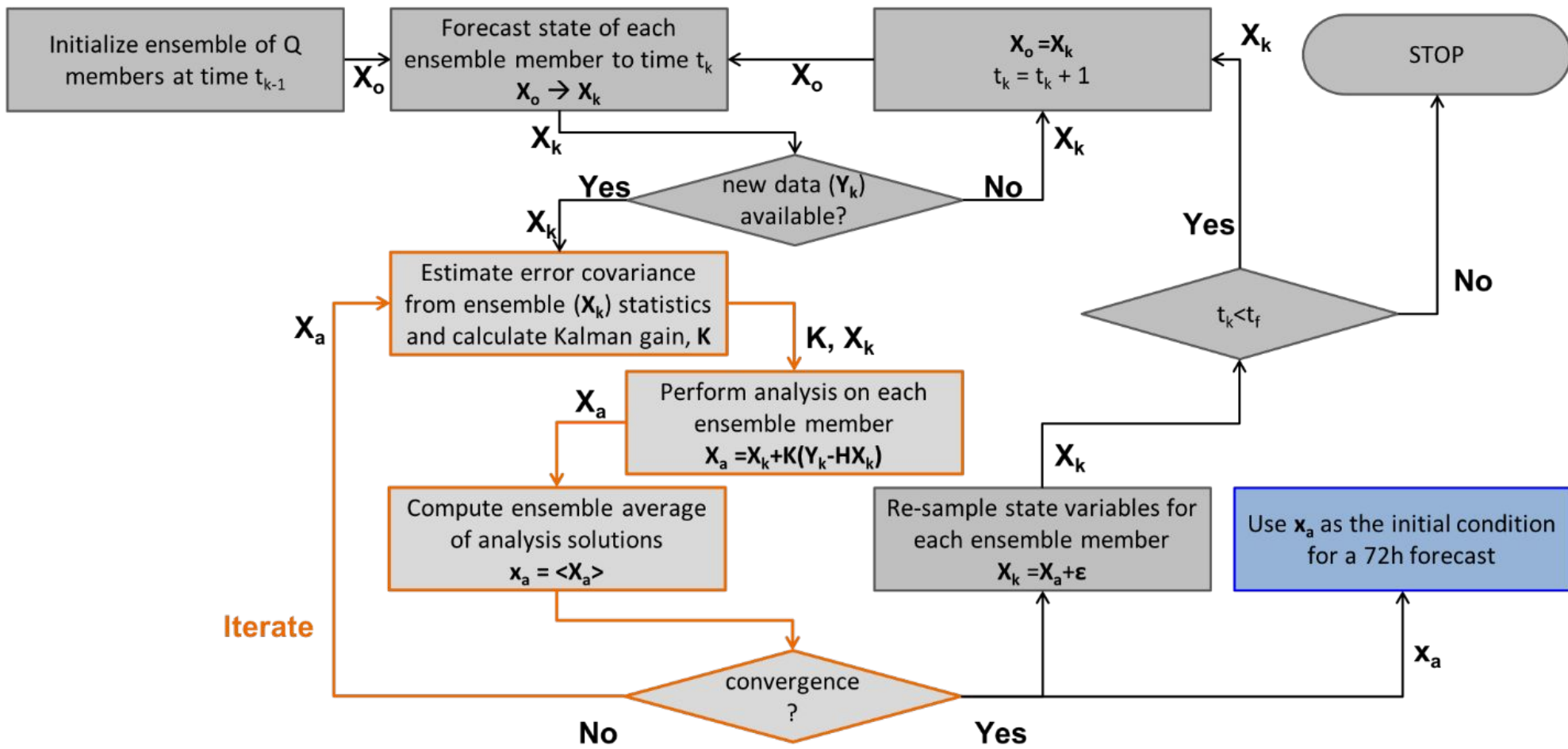


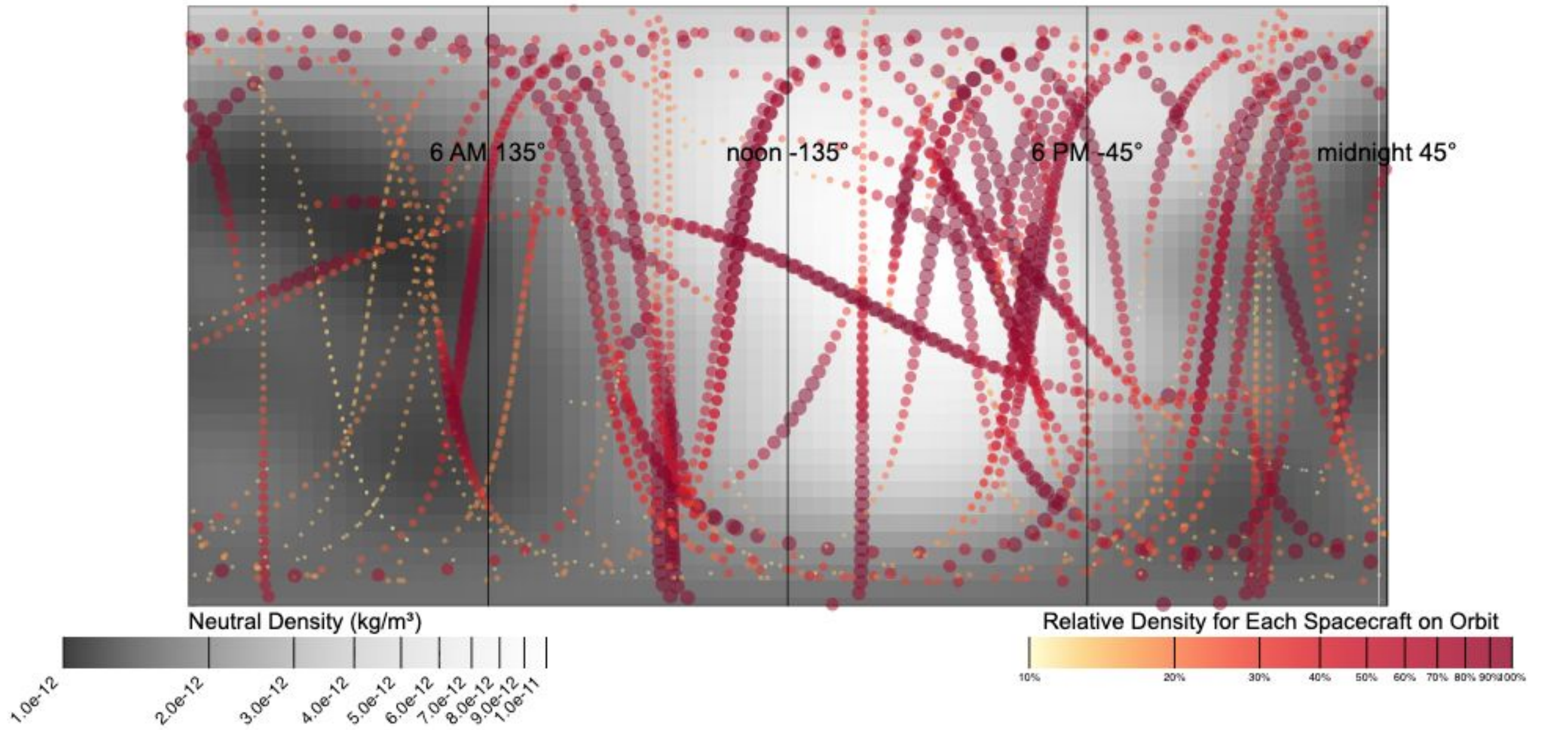
Blue Sky Thinking About Specifying and Forecasting the LEO Drag Environment

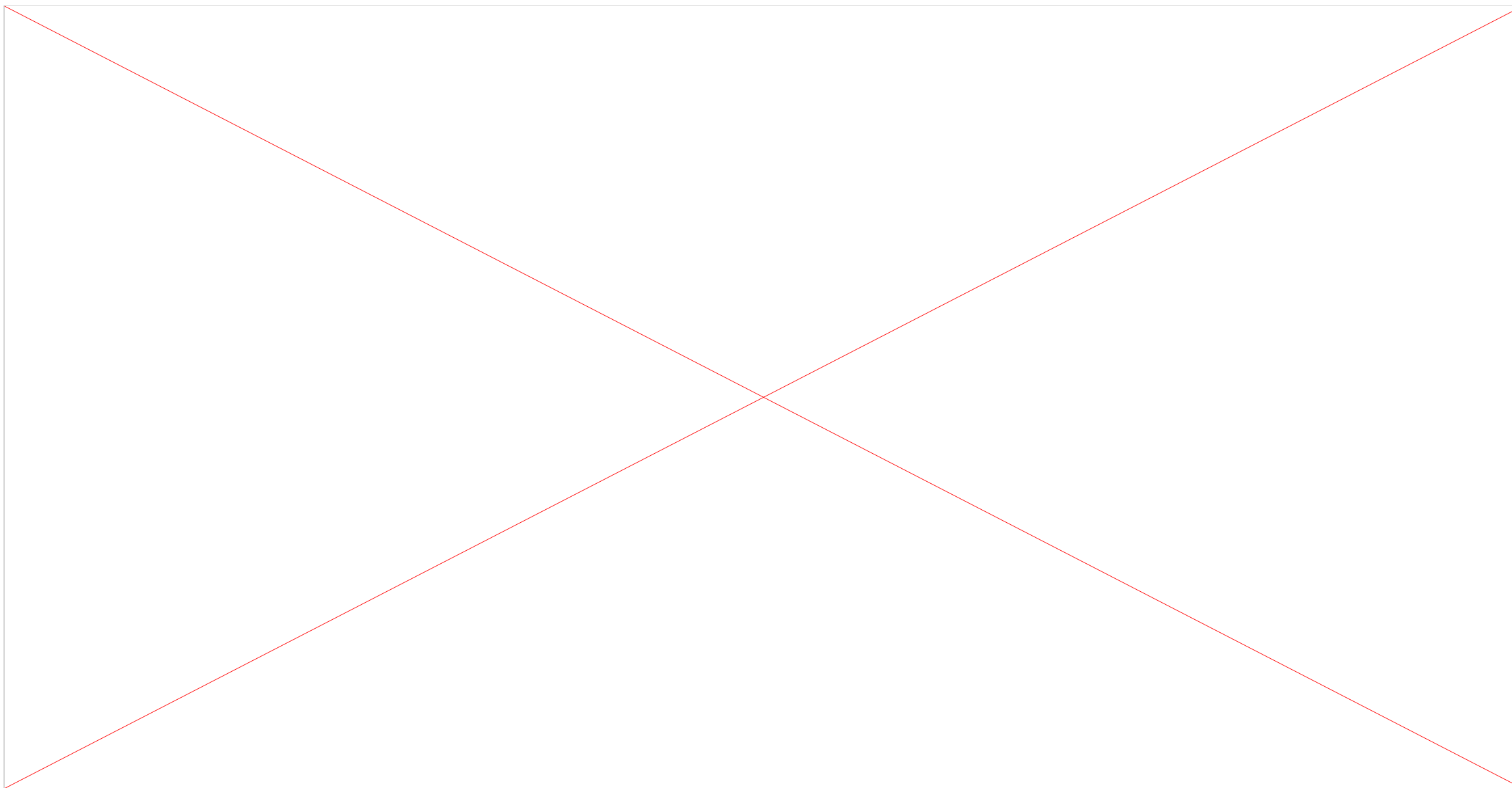
- How well do benefits of nowcast performance persist into the forecast?
- At what time scales does the importance of initial conditions (previous states) become relevant to the dynamic evolution of the thermosphere?
 - Under what conditions do GCM's offer benefits in the forecast over non-GCM's
- How do model quality and data coverage change nowcast (and forecast) quality?
 - When/where do we need more data?
 - How do we need to improve the models (and our understanding)?
 - At what time scales?

Thank You!

- Are the estimated forcing states and their variability physical?
To what extent?
- To what extent do they improve upon the operational indices/proxies?
- What are the estimation errors associated with the forcing states? To what extent are the geomagnetic vs. solar energy inputs observable?
- **How can the DA-based forcing estimates be leveraged to produce enhanced forecast inputs?**



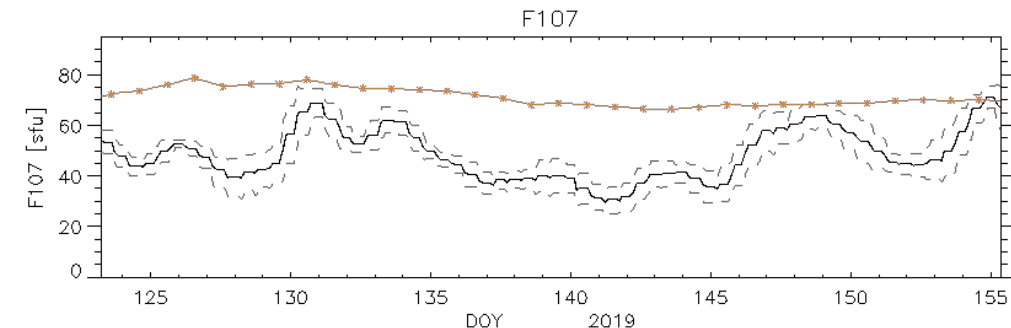
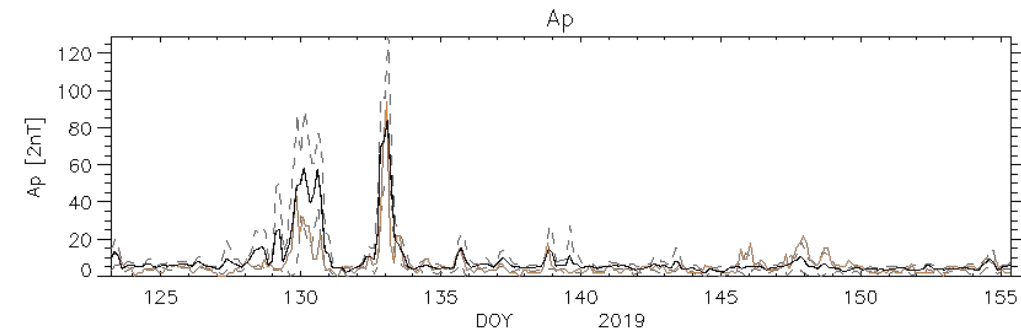
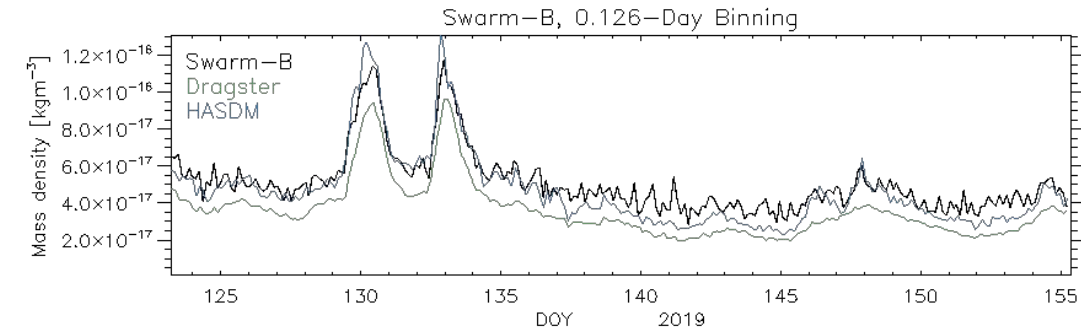
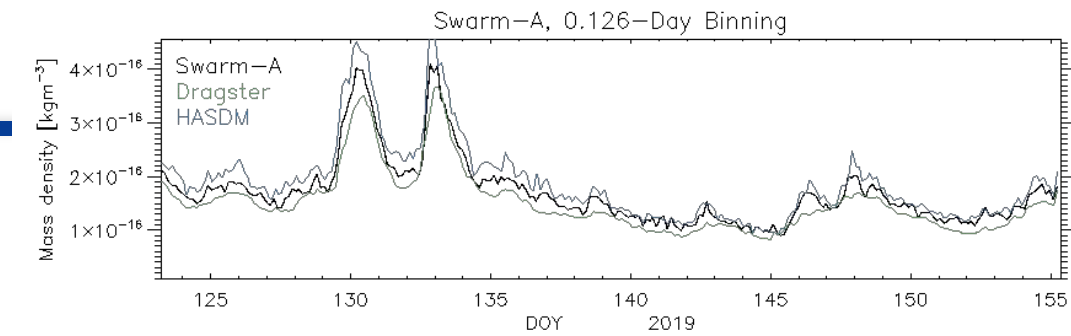




Dragster 2019 results

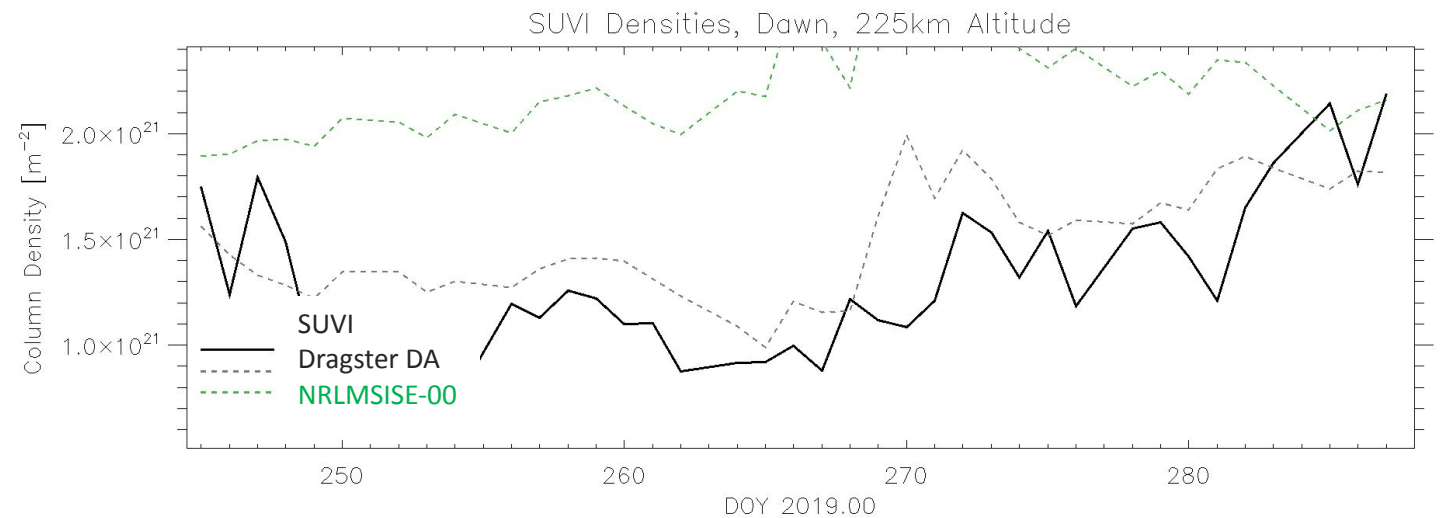
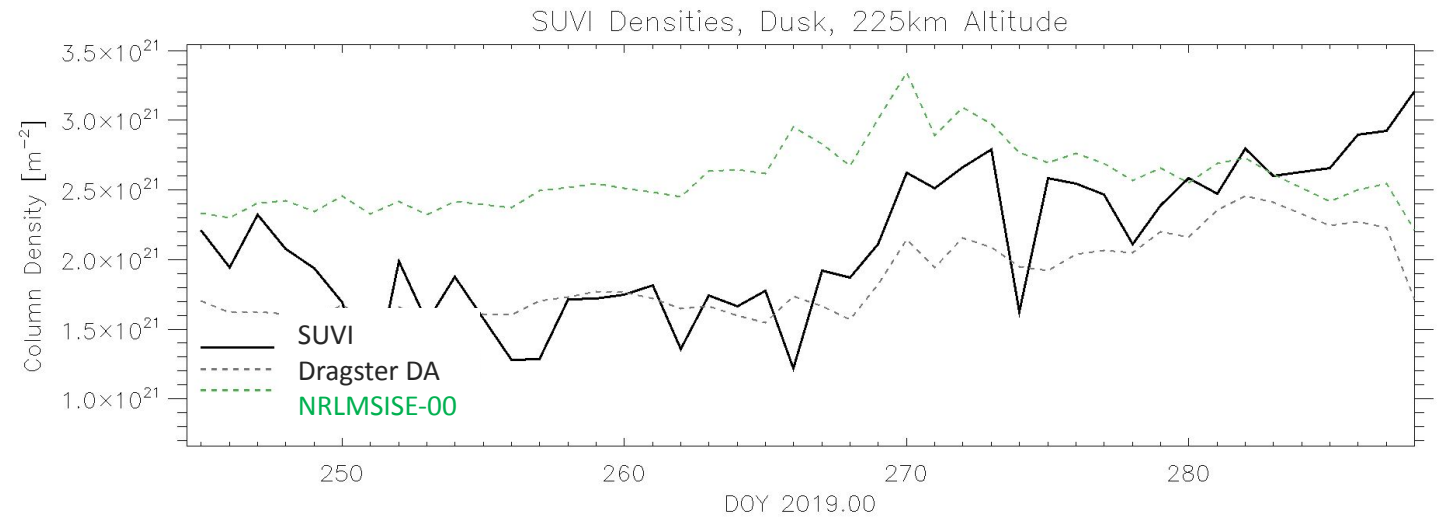
- Running around 20-30 x wallclock (on laptop M3 chipset)
- 50-70 satellites
- MSIS-2.1 background
 - 20 model ensemble members
 - 60 total
- 4-day assimilation windows
 - May want to consider 5
- Forecast launched every 12 hours
 - Changing this to 6 hours for future runs

| | Dragster log Std | HASDM log Std |
|---------|------------------|---------------|
| Swarm-A | 8.6% | 8.5% |
| Swarm-B | 20.0% | 20.4% |



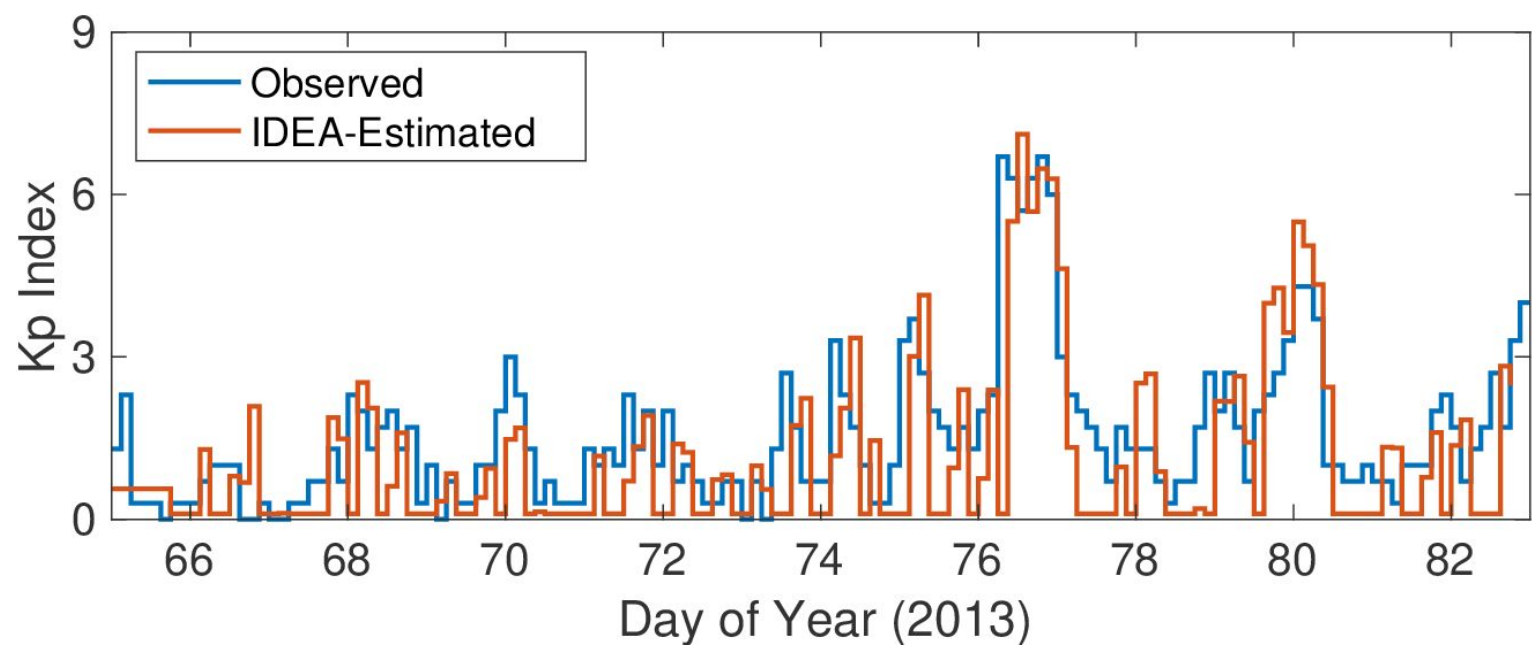
(mod-obs)/obs

| Altitude | Dawn MSIS STDEV | Dawn DA STDEV |
|----------|--------------------|------------------|
| 190 km | 54% | 23% |
| 195 km | 58% | 24% |
| 200 km | 56% | 23% |
| 225 km | 53% | 23% |
| 250 km | 50% | 23% |
| 275 km | 47% | 23% |
| 300 km | 47% | 24% |
| 325 km | 42% | 20% |
| 345 km | 44% | 22% |
| average: | 50% | 23% |



Courtesy of Robert Sewell and Ed Thiemann

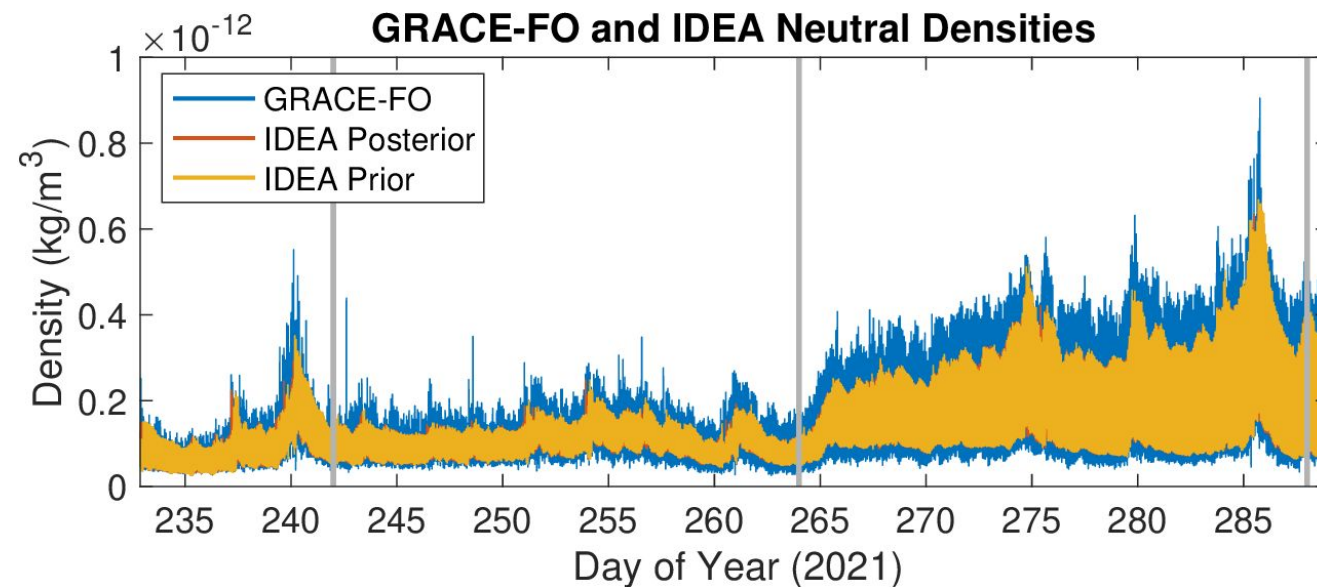
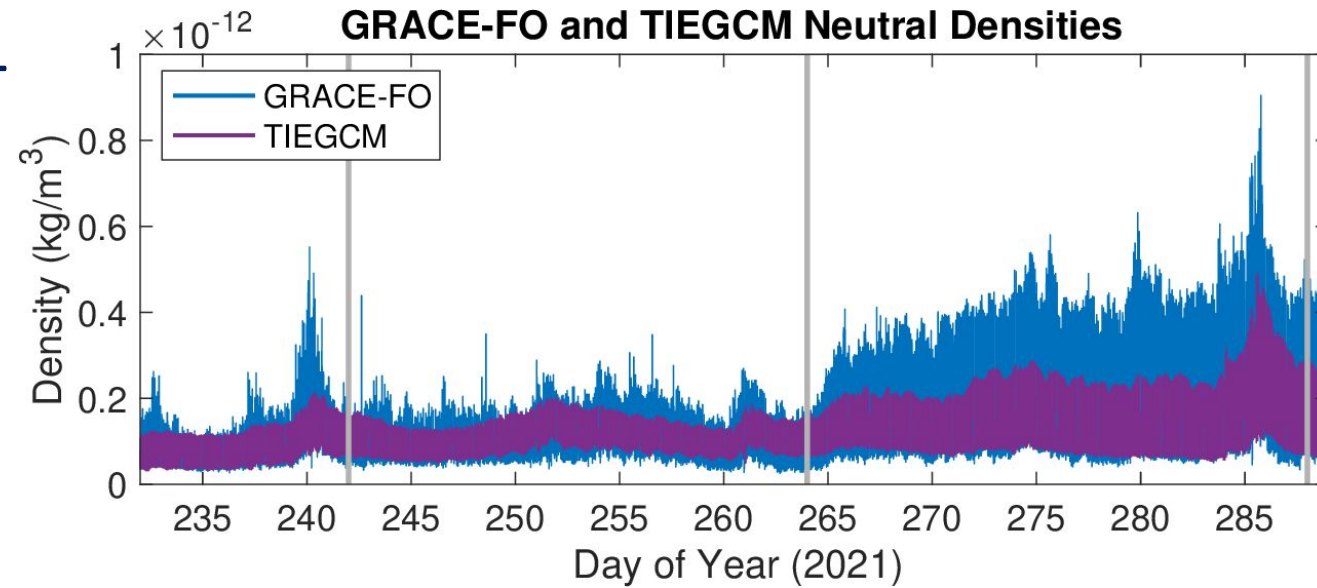
- Estimates corrections to external solar and geomagnetic drivers
- Ensembles of TIE-GCM models (can also use WAM-IPE)
- Has been shown to provide better or comparable densities to HASDM*

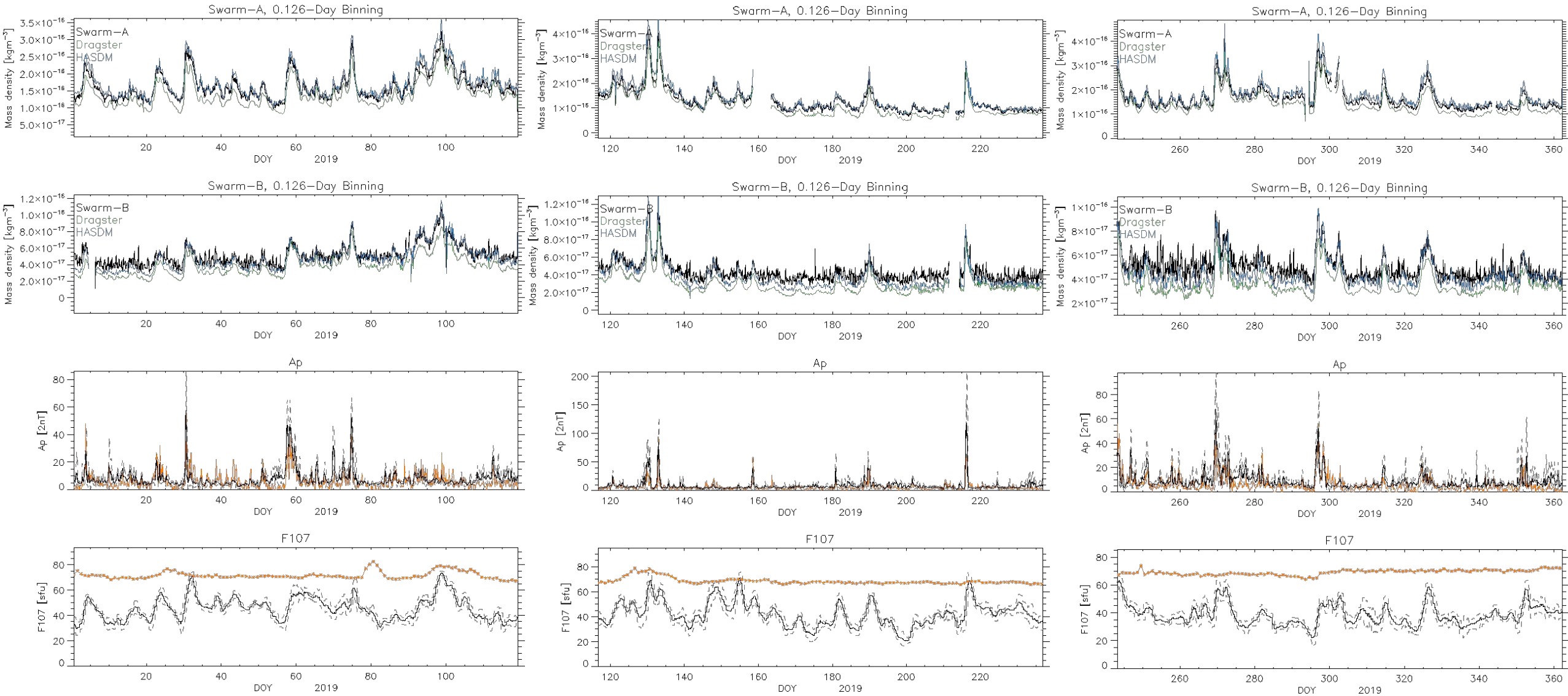


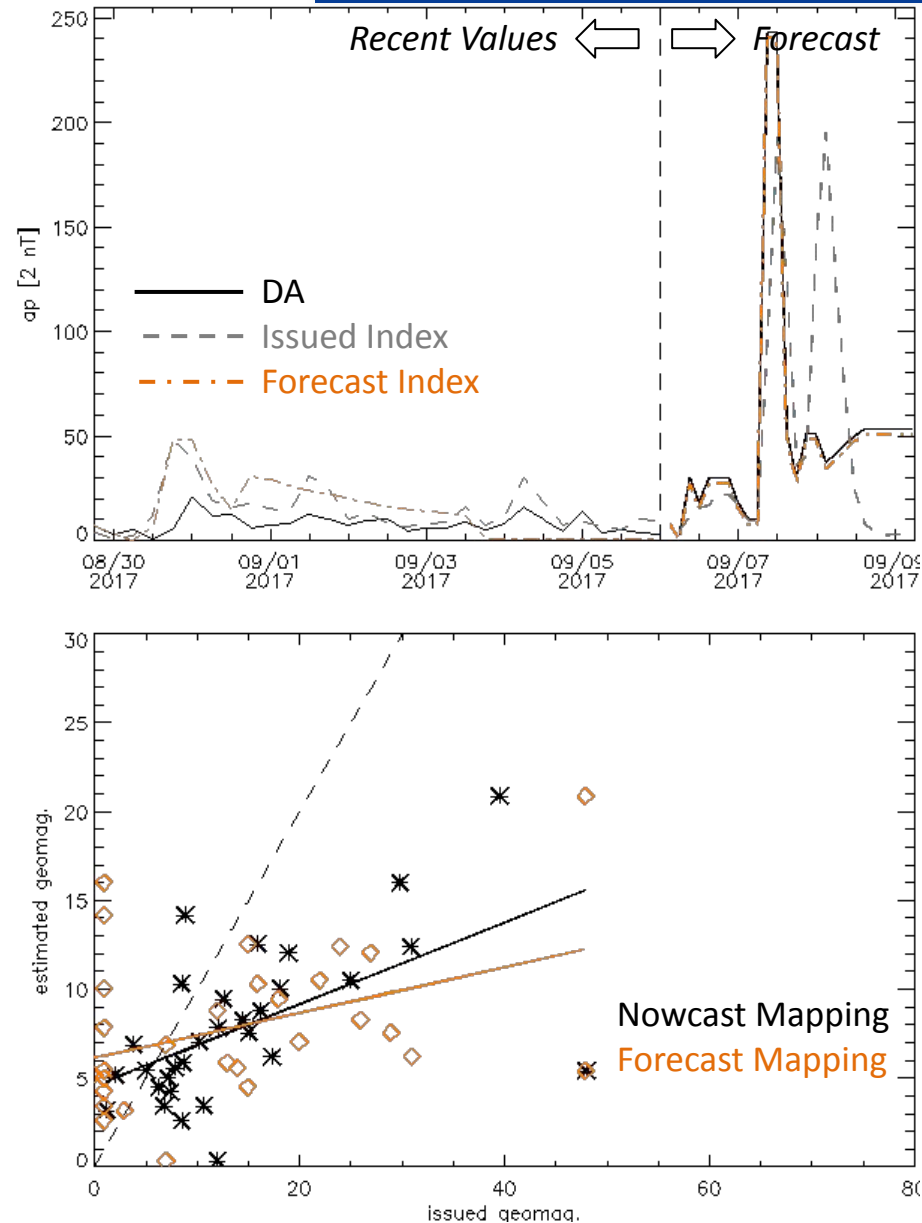
| 2003 day 80-365, Orbit Average – Ratio Validation Results, RMSe Logarithmic, 1 storm with Kp>5+ | | | | | |
|---|-------|--------|-------------|-------|-------------|
| | IDEA | HASDM* | TIE-GCM GPI | JB-08 | NRLMSISE-00 |
| GRACE-A | 0.076 | 0.072 | 0.273 | 0.172 | 0.266 |

*HASDM is the DoD operational, empirical, and data assimilative High Accuracy Satellite Drag Model

Sept. Equinox, 2021



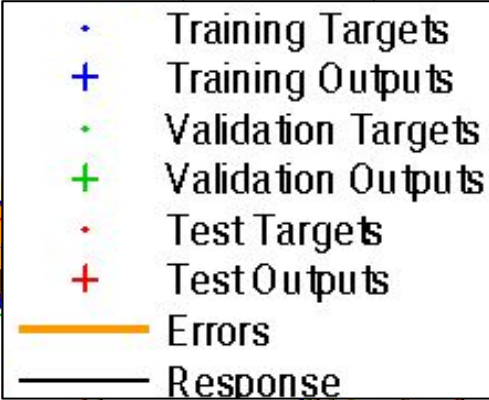
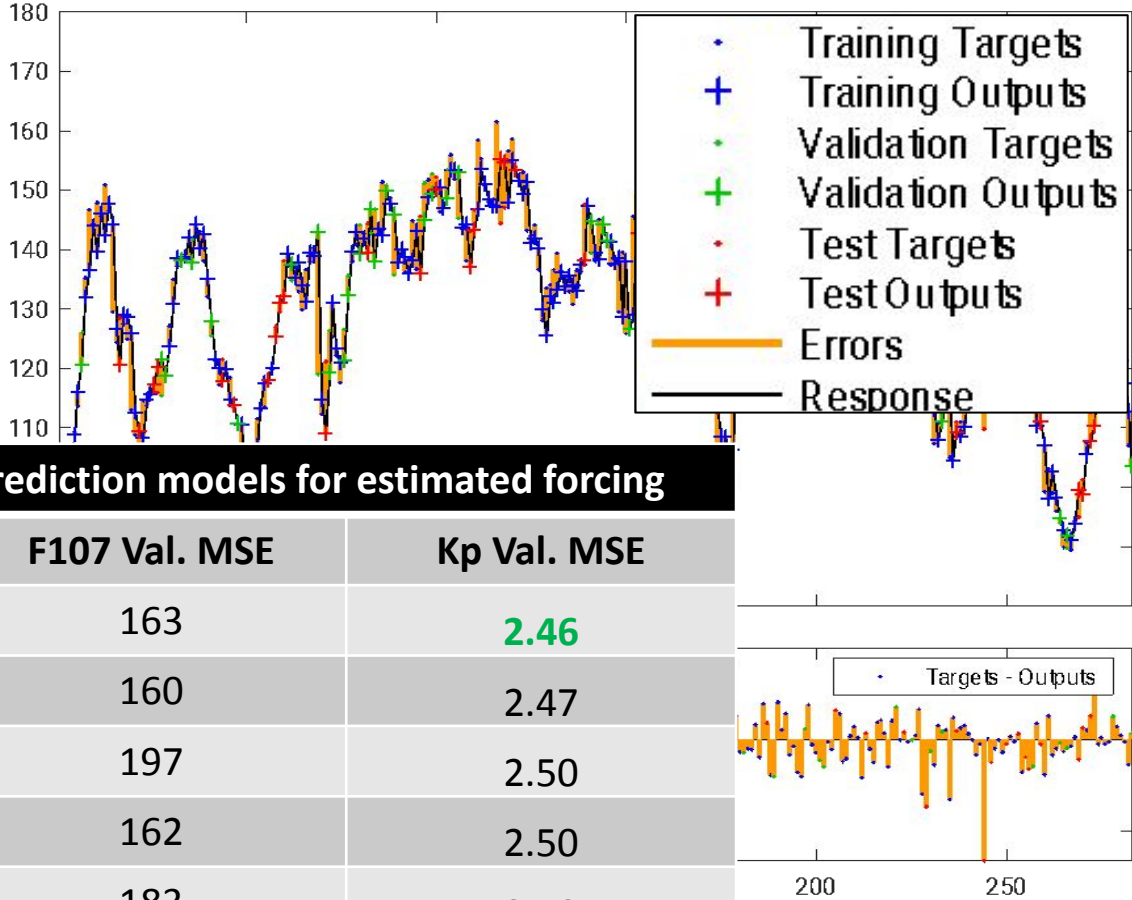
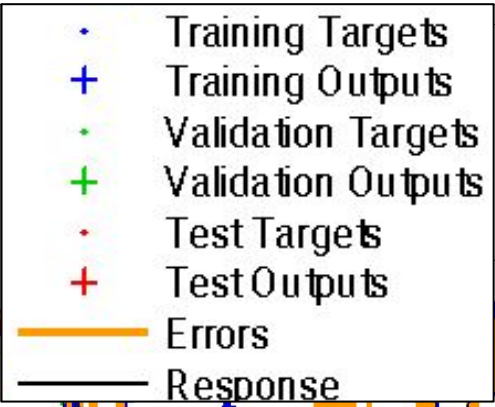
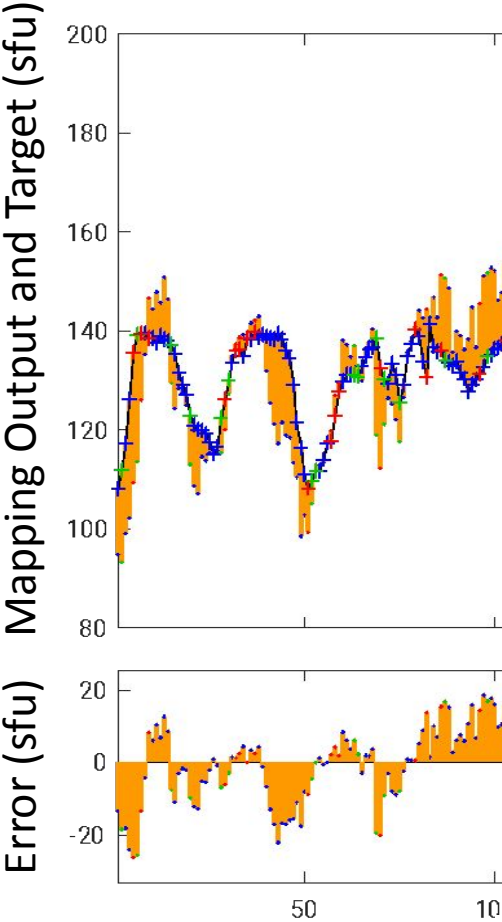




- Dragster and IDEA generate forecasts based on removing a bias between issued and forecast drivers at the time of the forecast launch.
- The bottom panel illustrates a linear-regression mapping of the recently issued nowcast (black) and forecast (orange) to the DA-estimated parameters. **This mapping changes with time and conditions.**
- Other neutral density forecasting approaches use bias offset or regression methods to compute forecasts
- ***How best to take advantage of recent DA driver estimates and recent forecast forcing performance?***

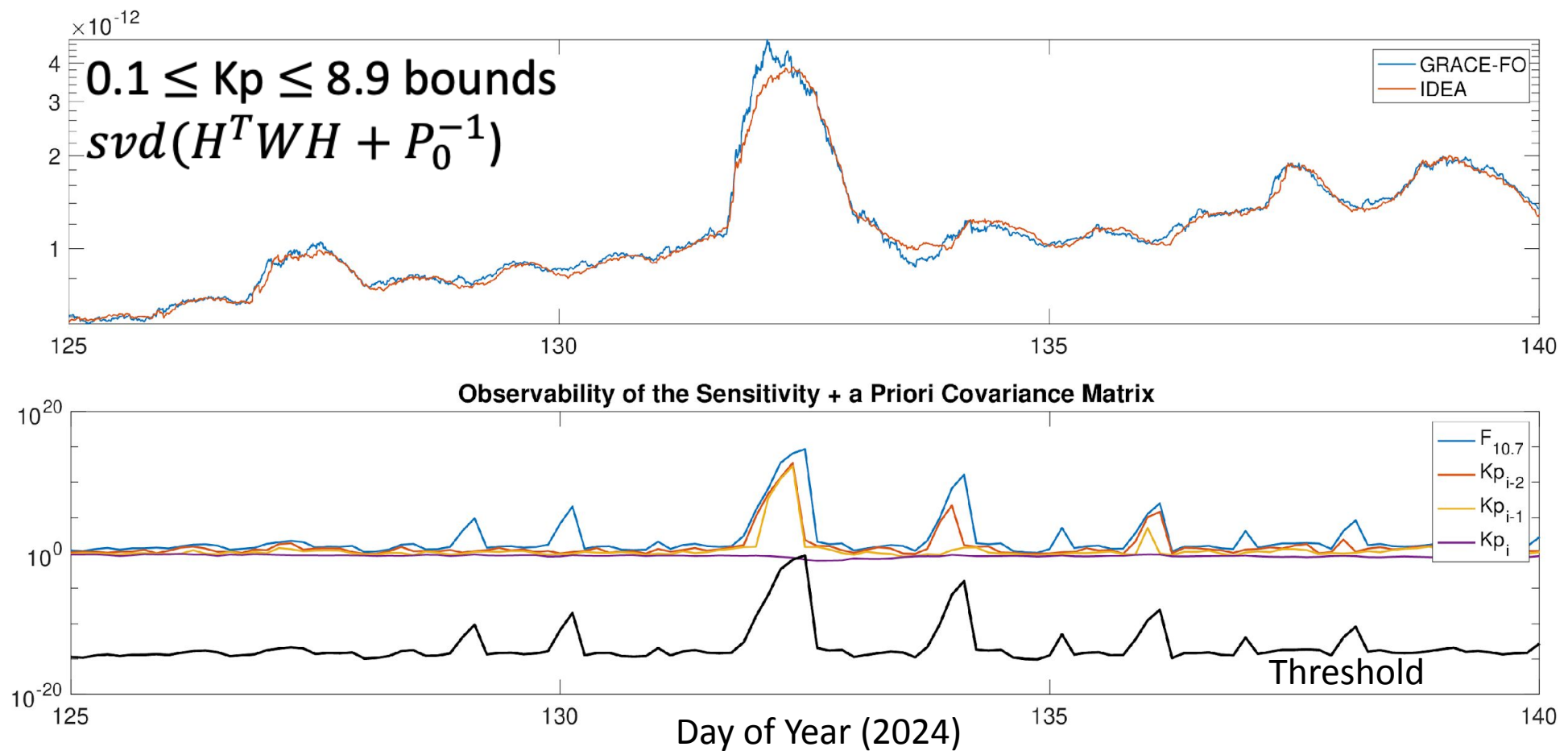
Nonlinear Autoregressive neural network, NAR
(MSE=163)

NARX using recent values of DA-estimated forcing
(MSE=37)

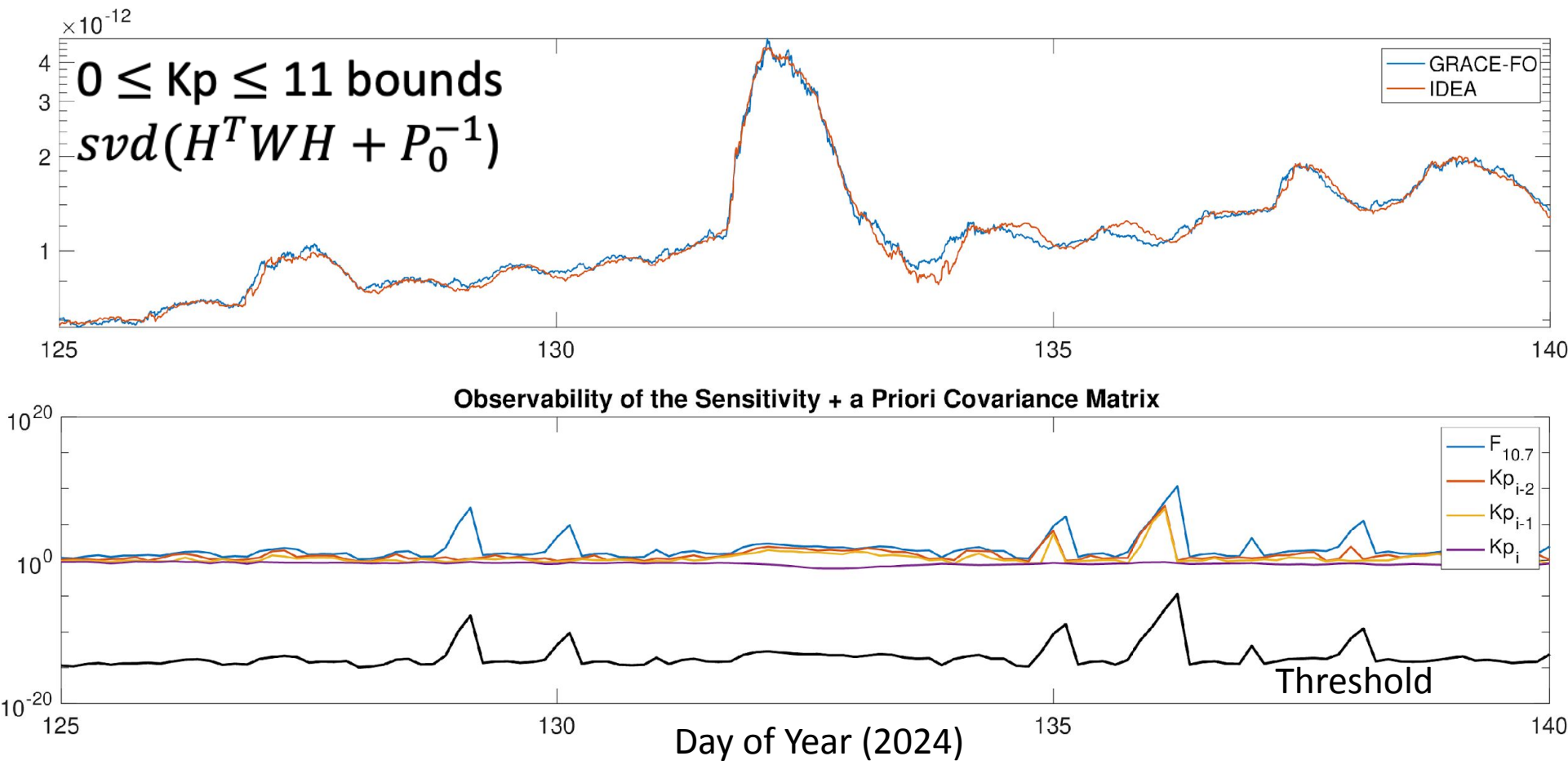


Validation of different regression prediction models for estimated forcing

| Model Type | F107 Val. MSE | Kp Val. MSE |
|--------------------------------|---------------|------------------|
| Neural Network | 163 | 2.46 |
| GPR | 160 | 2.47 |
| Ensemble | 197 | 2.50 |
| SVM | 162 | 2.50 |
| Tree | 183 | 2.50 |
| Linear Regression | 204 | 2.51 |
| Kernel | 294 | 3.42 |
| NARX using recent DA estimates | 37 | Under evaluation |



Threshold= $\max(svd(M)) * \dim(M) * eps$
 where $M = H^TWH + P_0^{-1}$



Threshold= $\max(svd(M)) * \dim(M) * eps$
 where $M = H^TWH + P_0^{-1}$

